


```

MM      MM      TTTTTTTTTT  HH      HH      HH      HH      CCCCCCCC  000000  SSSSSSSS  HH      HH
MM      MM      TTTTTTTTTT  HH      HH      HH      HH      CCCCCCCC  000000  SSSSSSSS  HH      HH
MMMM    MMMM    TT          HH      HH      HH      HH      CC          00      00      SS      HH      HH
MMMM    MMMM    TT          HH      HH      HH      HH      CC          00      00      SS      HH      HH
MM      MM      TT          HH      HH      HH      HH      CC          00      00      SS      HH      HH
MM      MM      TT          HH      HH      HH      HH      CC          00      00      SS      HH      HH
MM      MM      TT          HHHHHHHHHH  HHHHHHHHHH  CC          00      00      SSSSSS  HHHHHHHHHH
MM      MM      TT          HHHHHHHHHH  HHHHHHHHHH  CC          00      00      SSSSSS  HHHHHHHHHH
MM      MM      TT          HH      HH      HH      HH      CC          00      00      SS      HH      HH
MM      MM      TT          HH      HH      HH      HH      CC          00      00      SS      HH      HH
MM      MM      TT          HH      HH      HH      HH      CC          00      00      SS      HH      HH
MM      MM      TT          HH      HH      HH      HH      CC          00      00      SS      HH      HH
MM      MM      TT          HH      HH      HH      HH      CCCCCCCC  000000  SSSSSSSS  HH      HH
MM      MM      TT          HH      HH      HH      HH      CCCCCCCC  000000  SSSSSSSS  HH      HH

```

```

LL      IIIIII  SSSSSSSS
LL      IIIIII  SSSSSSSS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SSSSSS
LL      II      SSSSSS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SS
LLLLLLLLLLLL IIIIII  SSSSSSSS
LLLLLLLLLLLL IIIIII  SSSSSSSS

```

```

...
...
...
...

```

(2) 50
(3) 72
(4) 152

HISTORY ; Detailed Current Edit History
DECLARATIONS ; Declarative Part of Module
MT\$HCOSH - H Floating point COSH function

```

0000 1      .TITLE  MTH$HCOSH      ; H floating Hyperbolic Cosine routine
0000 2      ; (HCOSH)
0000 3      .IDENT /1-006/      ; File: MTHHCOSH.MAR      EDIT: RNH1006
0000 4
0000 5      :*****
0000 6      :*
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0000 22     :*  DIGITAL ASSUMES NO RESPONSIBILITY FOR THE USE OR RELIABILITY OF ITS
0000 23     :*  SOFTWARE ON EQUIPMENT WHICH IS NOT SUPPLIED BY DIGITAL.
0000 24     :*
0000 25     :*
0000 26     :*****
0000 27
0000 28
0000 29     : FACILITY: MATH LIBRARY
0000 30     :++
0000 31     : ABSTRACT:
0000 32
0000 33     : MTH$HCOSH is a function which returns the H floating hyperbolic cosine
0000 34     : of its H floating point argument. The call is standard
0000 35     : call-by-reference.
0000 36
0000 37     :--
0000 38
0000 39     : VERSION: 1
0000 40
0000 41     : HISTORY:
0000 42     : AUTHOR:
0000 43     :      John A. Wheeler, 12-Sep-1979: Version 1
0000 44
0000 45     : MODIFIED BY:
0000 46
0000 47
0000 48

```

```
0000 50      .SBTTL  HISTGRY ; Detailed Current Edit History
0000 51
0000 52
0000 53 ; Edit History for Version 1 of MTH$HCOSH
0000 54 :
0000 55 : 1-001 - Adapted from MTH$GCOSH.  JW 12-Sep-1979
0000 56 : 1-002 - Use MTH$HEXP R6.  SBL 4-Oct-1979
0000 57 : 1-003 - H_0.25 should be literal rather than own storage.  SBL 7-Oct-1979
0000 58 : 1-004 - Don't store reserved operand before signal.  SBL 7-Feb-1980
0000 59 : 1-005 - Changed lower limit for Chebyshev approximation from 2**56 to
0000 60 : 2**57.
0000 61 : - Eliminated second call to EXP for input values between .25 and
0000 62 : 57*ln2 by computing COSH(x) = (Z + 1/Z)/2, with Z = EXP(ixi)
0000 63 : - Eliminated second call to EXP for input values between 57*ln2
0000 64 : and 16383*ln2.
0000 65 : - Changed all final floating point divisions by 2 to interger
0000 66 : subtracts of 1 from the exponent field.
0000 67 : - Extended maximum range to 16384*ln2.
0000 68 : - Changed logic for computing EXP(ixi-ln2) to reduce error.
0000 69 : - RNH 10-FEB-81
0000 70 : 1-006 - Eliminated symbolic short literals.  RNH 15-Oct-81
```

```

0000 72      .SBTTL  DECLARATIONS      ; Declarative Part of Module
0000 73
0000 74      ;
0000 75      ; INCLUDE FILES:
0000 76      ;
0000 77      ; EXTERNAL SYMBOLS:
0000 78      .DSABL  GBL
0000 79      .EXTRN  MTH$$SIGNAL
0000 80      .EXTRN  MTH$K_FLOOVEMAT
0000 81      .EXTRN  MTH$HEXP_R6
0000 82      ;
0000 83      ; EQUATED SYMBOLS:
0000 84
0000 85
0000 86      ;
0000 87      ; MACROS:      none
0000 88      ;
0000 89
0000 90
0000 91      ;
0000 92      ; PSECT DECLARATIONS:
0000 93
0000 94      .PSECT  _MTH$CODE      PIC,SHR,LONG,EXE,NOWRT
0000 95      ; program section for math routines
0000 96      ;
0000 97      ; OWN STORAGE:  none
0000 98      ;
0000 99      ;
0000 100     ; CONSTANTS:
0000 101     ;
0000 102     ;
0000 103     H_16383_LOG_2:
E3E0A45E 62DE400E 0000 104     .QUAD  ^XE3E0A45E62DE400E
6B251812 C66964DB 0008 105     .QUAD  ^X6B251812C66964DB      ; 16383*ln2
0010 106     H_16384_LOG_2:
A39E2FEF 62E4400E 0010 107     .QUAD  ^XA39E2FEF62E4400E
07E66730 93C7F357 0018 108     .QUAD  ^X07E6673093C7F357      ; 16384*ln2
0020 109     H_LOG_2_HI:
A39E2FEF 62E44000 0020 110     .QUAD  ^XA39E2FEF62E44000
40006730 93C7F357 0028 111     .QUAD  ^X4000673093C7F357      ; (high 109 bits of ln2)+2*-109
0030 112     H_LOG_2_LO:
FOCB950B C0D0BF9D 0030 113     .QUAD  ^XFOCB950BC0D0BF9D
5F359D27 D674CD98 0038 114     .QUAD  ^X5F359D27D674CD98      ; ln2 - H_LOG_2_HI
0040 115     H_2_POWER_57:
00000000 0000403A 0040 116     .QUAD  ^X0000000000000403A
00000000 00000000 0048 117     .QUAD  0      ; 2*57
0050 118
0050 119     HCOSHTAB:
2B3EE172 8C8F3FAB 0050 120     .LONG  ^X8C8F3FAB,^X2B3EE172      ; 2.502658279567823990162458156254711E -27
ADEB4F57 5BD2E986 0058 121     .LONG  ^X5BD2E986,^XADEB4F57
D01949AF F2C93FB1 0060 122     .LONG  ^XF2C93FB1,^XD01949AF      ; 1.611665395066462480330719767236559E -24
C60346B9 1DF63B8C 0068 123     .LONG  ^X1DF63B8C,^XC60346B9
64FF997D 0CE33FBB 0070 124     .LONG  ^X0CE33FBB,^X64FF997D      ; 8.896792721476872237647982378253568E -22
7CB38AA4 0B3F40F3 0078 125     .LONG  ^X0B3F40F3,^X7CB38AA4
F4FDBA3C E5423FC3 0080 126     .LONG  ^XE5423FC3,^XF4FDBA3C      ; 4.110317621712466937445902717251860E -19
60105113 6DEFA6F1 0088 127     .LONG  ^X6DEFA6F1,^X60105113
9928863B 68273FCC 0090 128     .LONG  ^X68273FCC,^X9928863B      ; 1.561920696859944528721805191130865E -16

```

E533A92E	54A49ACF	0098	129	.LONG	^X54A49ACF, ^XE533A92E		
3B813E73	AE7F3FD4	00A0	130	.LONG	^XAE7F3FD4, ^X3B813E73	:	4.779477332387377634901255174808471E -14
4B6B3FDC	D10B2ED8	00A8	131	.LONG	^XD10B2ED8, ^X4B6B3FDC		
07C94A8C	93973FDC	00B0	132	.LONG	^X93973FDC, ^X07C94A8C	:	1.147074559772972474513234083768590E -11
7DE98CBB	FC3DD25A	00B8	133	.LONG	^XFC3DD25A, ^X7DE98CBB		
8D898EFF	1EED3FE4	00C0	134	.LONG	^X1EED3FE4, ^X8D898EFF	:	2.087675698786809897912112497212423E -9
85215944	371B7B54	00C8	135	.LONG	^X371B7B54, ^X85215944		
89F5FB77	27E43FEB	00D0	136	.LONG	^X27E43FEB, ^X89F5FB77	:	2.755731922398589065255749092851911E -7
94EA88C4	F01FC72E	00D8	137	.LONG	^XF01FC72E, ^X94EA88C4		
1A0101A0	A01A3FF1	00E0	138	.LONG	^XA01A3FF1, ^X1A0101A0	:	2.480158730158730158730158708693922E -5
1BE015A7	01A0A01A	00E8	139	.LONG	^X01A0A01A, ^X1BE015A7		
16C1C16C	6C163FF7	00F0	140	.LONG	^X6C163FF7, ^X16C1C16C	:	1.388888888888888888888888888904959E -3
B9DF16C2	C16C6C16	00F8	141	.LONG	^XC16C6C16, ^XB9DF16C2		
55555555	55553FFC	0100	142	.LONG	^X55553FFC, ^X55555555	:	4.16666666666666666666666666666603E -2
54ED5555	55555555	0108	143	.LONG	^X55555555, ^X54ED5555		
00000000	00004000	0110	144	.LONG	^X00004000, ^X00000000	:	5.00000000000000000000000000000000E -1
00000000	00000000	0118	145	.LONG	^X00000000, ^X00000000		
00000000	00004001	0120	146	.LONG	^X00004001, ^X00000000	:	9.99999999999999999999999999999999E -1
00000000	00000000	0128	147	.LONG	^X00000000, ^X00000000		
		0130	148				
	0000000E	0130	149	HCOSHTAB/16	= .- HCOSHTAB/16		
		0130	150				

```

0130 152          .SBTTL MTH$HCOSH - H Floating point COSH function
0130 153
0130 154
0130 155 :++
0130 156 : FUNCTIONAL DESCRIPTION:
0130 157 :
0130 158 : HCOSH - double precision H floating point function
0130 159 :
0130 160 : HCOSH(X) is computed as:
0130 161 :
0130 162 :     If |X| < 2*-57, HCOSH(X) = 1.
0130 163 :     If 2*-57 <= |X| < 0.25, HCOSH(X) = Chebyshev series
0130 164 :     If 0.25 <= |X| < 57*ln2, let Z = HEXP(|X|) and set HCOSH(X) = (Z+1/Z)/2
0130 165 :     If 57*ln2 <= |X| < 16383*ln2, then HCOSH(X) = HEXP(|X|)/2.
0130 166 :     If 16383*ln2 <= |X| < 16384*ln2, then HCOSH(X) = HEXP(|X|-ln2).
0130 167 :     If 16384*ln2 <= |X|, then overflow.
0130 168 :
0130 169 : CALLING SEQUENCE:
0130 170 :
0130 171 :     hcosh.wh.v = MTH$HCOSH(x.rh.r)
0130 172 :
0130 173 :     -or-
0130 174 :
0130 175 :     CALL MTH$HCOSH(hcosh.wh.r, x.rh.r)
0130 176 :
0130 177 :     Because an H-floating result cannot be expressed in 64 bits, it is
0130 178 :     returned as the first argument, with the input parameter displaced
0130 179 :     to the second argument, in accordance with the Procedure Calling
0130 180 :
0130 181 :
0130 182 : INPUT PARAMETERS:
0130 183 :
00000004 0130 184 :     LONG = 4 ; define longword multiplier
00000008 0130 185 :     x = 2 * LONG ; Contents of x is the argument
0130 186 :
0130 187 : IMPLICIT INPUTS: none
0130 188 :
0130 189 : OUTPUT PARAMETERS:
00000004 0130 190 :
0130 191 :     hcosh = 1 * LONG
0130 192 :
0130 193 : IMPLICIT OUTPUTS: none
0130 194 :
0130 195 : COMPLETION CODES: none
0130 196 :
0130 197 : SIDE EFFECTS:
0130 198 :
0130 199 : Signal: MTH$ FLOOVEMAT if 16384*ln2 <= |X| with reserved operand in R0/R3
0130 200 : (copied to the signal mechanism vector CHF$L_MCH_R0/R1 by LIB$SIGNAL).
0130 201 : Associated message is: "FLOATING OVERFLOW IN MATH LIBRARY". Result is reserved
0130 202 : operand -0.0 unless a user supplied (or any) error handler changes CHF$L_MCH_R0/R1
0130 203 :
0130 204 : NOTE: This procedure disables floating point underflow, enables integer
0130 205 : overflow.
0130 206 :
0130 207 : ---
0130 208

```



```

0130 209
40FC 0130 210 .ENTRY MTH$HCOSH, ^M<IV, R2, R3, R4, R5, R6, R7 >
0132 211 : standard call-by-reference entry
0132 212 : disable DV (and FU), enable IV
0132 213 MTH$FLAG_JACKET : flag that this is a jacket procedure in
0132
6D 00000000'GF 9E 0132 MOVAB G^MTH$$JACKET_HND, (FP)
0139 : set handler address to jacket
0139 : handler
0139
6D 00000000'GF 9E 0139 214 : case of an error in routine
0139 215 MOVAB G^MTH$$JACKET_HND, (FP) : Set handler address to jacket handler
0140 216 : If an error, convert signal to user PC
0140 217 : and resignal
50 08 BC 70FD 0140 218 MOVH @x(AP), R0 : R0/R3 = |X| = @value(AP)
50 8000 8F AA 0145 219 BICW2 #^X8000, R0 : R0/R3 = |X|
3FFF 8F 50 B1 014A 220 CMPW R0, #^X3FFF : compare |X| with 0.25
1E 18 014F 221 BGEQ GEQ_TO_0.25 : branch if |X| >= 0.25
0151 222
0151 223 :
0151 224 : |X| < 0.25
0151 225 :
0151 226
3FC8 8F 50 B1 0151 227 CMPW R0, #^X3FC8 : compare |X| with 2*-57
06 18 0156 228 BGEQ GEQ_TO_2M57 : branch if |X| >= 2*-57
0158 229
0158 230 :
0158 231 : |X| < 2*-57
0158 232 :
0158 233
04 BC 08 70FD 0158 234 MOVH #1, @hcosh(AP) : Store 1.0 as result
04 04 015D 235 RET : return
015E 236
015E 237 :
015E 238 : 2*-57 =< |X| < 0.25
015E 239 :
015E 240
015E 241 GEQ_TO_2M57:
FEE7 CF 50 50 64FD 015E 242 MULH2 R0,R0 :Get ARG*2 for POLYH.
50 75FD 0162 243 POLYH R0, #HCOSHLLEN-1, HCOSHTAB
04 BC 50 70FD 0169 244 : R0/R3 = SUM(Ci*X^i)
04 04 0169 245 MOVH R0, @hcosh(AP) : Store result in first argument
016E 246 RET : return
016F 247
016F 248 :
016F 249 : 0.25 =< |X|
016F 250 :
016F 251
016F 252 GEQ_TO_0.25:
FE8B CF 50 71FD 016F 253 CMPH R0, H 16383 LOG_2 : compare |X| with 16383*ln2
20 14 0175 254 BGTR GTR_TRAN_16383_LOG_2 : branch if |X| > 16383*ln2
0177 255
0177 256 :
0177 257 : 0.25 =< |X| =< 16383*ln2
0177 258 :
0177 259
00000000'EF 16 0177 260 JSB MTH$HEXP_R6 : R0/R3 = HEXP(|X|)

```

```

FEBD CF 50 71FD 017D 261      CMPH    R0, H 2 POWER_57      : Compare HEXP(!X!) with 2*57, if
09 14 0183 262      BGTR    ONE_TERM_ONLY-      : larger, only one term is needed.
54 08 50 67FD 0185 263      DIVH3   R0, #1, R4          : R4/R7 = HEXP(-!X!)
50 54 60FD 018A 264      ADDH2   R4, R0             : R0/R3 = HEXP(X) + HEXP(-X)
018E 265      ONE_TERM ONLY:
04 50 01 A2 018E 266      SUBW2   #^X0001, R0        : R0/R3 = (HEXP(X) + HEXP(-X))/2
50 7DFD 0191 267      MOVO    R0, @hcosh(AP)     : move COSH(x) to first argument
04 BC 50 04 0196 268      RET                                : and return
0197 269
0197 270
0197 271      : 16383*ln2 < !X!
0197 272
0197 273
0197 274      GTR_THAN 16383_LOG_2:
FE73 CF 50 71FD 0197 275      CMPH    R0, H_16384_LOG_2  : compare !X! with 16384*ln2
1A 18 019D 276      BGEQ    ERROR            : branch to ERROR if 16384*ln2 =<!X!
019F 277
019F 278
019F 279      : 16383*ln2 =< !X! < 16384*ln2
019F 280
019F 281
019F 282
50 FE7C CF 62FD 019F 283      SUBH2   H_LOG_2_HI, R0    : R0/R3=!X!-(hi 109 bits of ln2+2*-109)
00000000'EF 16 01A5 284      JSB     MTH$HEXP_R6      : R0/R3=HEXP(!X!-H_LOG_2_HI)
54 50 FE80 CF 65FD 01AB 285      MULH3   H_LOG_2_LO, R0, R4 : R4/R7=H_LOG_2_LO*HEXP(!X!-H_LOG_2_LO)
04 BC 50 54 61FD 01B2 286      ADDH3   R4, R0, @hcosh(AP) : Store HEXP(!X!-ln2) in 1st argument
04 04 01B8 287      RET                                : return
01B9 288
01B9 289      : 16383*ln2 + LOG(2) =< !X!, error
01B9 290
01B9 291
01B9 292
7E 00'8F 9A 01B9 293      ERROR: MOVZBL #MTH$K_FLOOVEMAT, -(SP) : condition value
50 01 0F 79 01BD 294      ASHQ    #15, #T, R0      : R0 = result = reserved operand -0.0
01C1 295
01C1 296
00000000'EF 52 7C 01C1 297      CLRQ    R2
04 BC 01 FB 01C3 298      CALLS   #1, MTH$$$SIGNAL : signal error and use real user's PC
04 BC 50 7DFD 01CA 299      MOVO    R0, @hcosh(AP)   : Restore result
01CF 300      RET                                : return
01D0 301
01D0 302
01D0 303
01D0 304      .END

```

MTH\$HCOSH
Symbol table

K 15
; H floating Hyperbolic Cosine routine

16-SEP-1984 01:35:02
6-SEP-1984 11:24:49

VAX/VMS Macro V04-00
[MTHRTL.SRC]MTHHCOSH.MAR;1

Page 8
(4)

MTH
1-(

```

ERROR          000001B9 R    01
GEQ_TO_0.25    0000016F R    01
GEQ_TO_2M57    0000015E R    01
GTR_THAN_16383_LOG_2 00000197 R    01
HCOSH          = 00000004
HCOSHLEN       = 0000000E
HCOSHTAB       00000050 R    01
H_16383_LOG_2  00000000 RR   01
H_16384_LOG_2  00000010 RR   01
H_2_POWER_57   00000040 R    01
H_LOG_2_HI     00000020 R    01
H_LOG_2_LO     00000030 R    01
LONG          = 00000004
MTH$$JACKET_HND ***** X    01
MTH$$SIGNAL    ***** X    00
MTH$HCOSH      00000130 RG   01
MTH$HEXP_R6    ***** X    00
MTH$K_FLOOVMAT ***** X    00
ONE_TERM_ONLY  0000018E R    01
X              = 00000008
  
```

! Psect synopsis !

PSECT name	Allocation	PSECT No.	Attributes
ABS	00000000 (0.)	00 (0.)	NOPIC USR CON ABS LCL NOSHR NOEXE NORD NOWRT NOVEC BYTE
_MTH\$CODE	000001D0 (464.)	01 (1.)	PIC USR CON REL LCL SHR EXE RD NOWRT NGVEC LONG

! Performance indicators !

Phase	Page faults	CPU Time	Elapsed Time
Initialization	32	00:00:00.07	00:00:01.11
Command processing	126	00:00:00.68	00:00:03.06
Pass 1	91	00:00:01.06	00:00:04.74
Symbol table sort	0	00:00:00.00	00:00:00.00
Pass 2	66	00:00:00.78	00:00:02.77
Symbol table output	4	00:00:00.02	00:00:00.02
Psect synopsis output	3	00:00:00.02	00:00:00.12
Cross-reference output	0	00:00:00.00	00:00:00.00
Assembler run totals	324	00:00:02.64	00:00:11.85

The working set limit was 900 pages.
 4622 bytes (10 pages) of virtual memory were used to buffer the intermediate code.
 There were 10 pages of symbol table space allocated to hold 20 non-local and 0 local symbols.
 364 source lines were read in Pass 1, producing 11 object records in Pass 2.
 1 page of virtual memory was used to define 1 macro.

+-----+
: Macro library statistics !
+-----+

Macro library name	Macros defined
-----	-----
_\$255\$DUA28:[SYSLIB]STARLET.MLB;2	0

0 GETS were required to define 0 macros.

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL,TRACEBACK)/LIS=LIS\$:MTHHCOSH/OBJ=OBJ\$:MTHHCOSH MSRCS:MTHJACKET/UPDATE=(ENH\$:MTHJACKET)+MSRC

