

| | |
|-----|-----|
| (2) | 54 |
| (3) | 69 |
| (4) | 113 |
| (5) | 176 |
| (6) | 267 |
| (7) | 330 |

| | |
|---------------|---------------------------------|
| HISTORY | : Detailed Current Edit History |
| DECLARATIONS | : Declarative Part of Module |
| MTHSGACOS | - Standard G Floating GACOS |
| MTHSGACOS_R7 | - Special GACOS routine |
| MTHSGACOSD | - Standard G Floating GACOSD |
| MTHSGACOSD_R7 | - Special GACOSD routine |

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0000 1      .TITLE  MTH$GACOS      : G Floating Point Arc-cosine routine
0000 2      : (GACOS,GACOSD)
0000 3      .IDENT /1-006/      : File: MTHGACOS.MAR  EDIT: RNH1006
0000 4      :
0000 5      :*****
0000 6      :*
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0000 23     :*  SOFTWARE ON EQUIPMENT WHICH IS NOT SUPPLIED BY DIGITAL.
0000 24     :*
0000 25     :*
0000 26     :*****
0000 27     :
0000 28     :
0000 29     : FACILITY: MATH LIBRARY
0000 30     :++
0000 31     : ABSTRACT:
0000 32     :
0000 33     : MTH$GACOS is a function which returns the G floating point arc-cosine
0000 34     : in radians of its G floating point argument. The call is standard
0000 35     : call-by-reference.
0000 36     :
0000 37     : MTH$GACOSD is a function which returns the G floating point arc-cosine
0000 38     : in degrees of its G floating point argument. The call is standard
0000 39     : call-by-reference.
0000 40     :
0000 41     :--
0000 42     :
0000 43     : VERSION: 1
0000 44     :
0000 45     : HISTORY:
0000 46     : AUTHOR:
0000 47     :     Steven B. Lionel, 15-Jan-79: Version 1
0000 48     :
0000 49     : MODIFIED BY:
0000 50     :
0000 51     :
0000 52     :

```

MTH\$GACOS
1-006

N 4

; G Floating Point Arc-cosine routine 16-SEP-1984 01:24:21 VAX/VMS Macro V04-00
HISTORY ; Detailed Current Edit History 6-SEP-1984 11:23:16 [MTHRTL.SRC]MTHGACOS.MAR;1

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(2)

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0000 54 .SBTTL HISTORY ; Detailed Current Edit History
0000 55
0000 56
0000 57 ; ALGORITHMIC DIFFERENCES FROM FP-11/C ROUTINE: none
0000 58 ;
0000 59 ; Edit History for Version 1 of MTH$GACOS
0000 60 ;
0000 61 ; 1-001 - Adapted from MTH$DACOS version 1-001. SBL 15-Jan-79
0000 62 ; 1-002 - Change JSB entry to MTH$GACOS R7. RBG 28-Sept-1979
0000 63 ; 1-003 - Added degree entry points. RNH 22-MAR-1981
0000 64 ; 1-004 - Modified computation of  $1 - X^2$  to avoid loss of significance
0000 65 ; for  $|X| \geq 1/2$ . RNH 02-Sept-1981
0000 66 ; 1-005 - Changed shared external references to G^. RNH 02-Oct-81
0000 67 ; 1-006 - Eliminated symbolic short literals. RNH 15-Oct-81
```

```
0000 69 .SBTTL DECLARATIONS ; Declarative Part of Module
0000 70
0000 71 :
0000 72 : INCLUDE FILES: JTSPARAMS.MAR
0000 73 :
0000 74 : EXTERNAL SYMBOLS:
0000 75 :
0000 76
0000 77 .DSABL GBL ; force undefines to error
0000 78 .EXTRN MTHSGATAN R7 ; arctangent routine
0000 79 .EXTRN MTHSGATAN_D R7 ; arctangent routine
0000 80 .EXTRN MTHSGSQRT R5 ; square root routine
0000 81 .EXTRN MTHSSIGNAL ; math signal routine
0000 82 .EXTRN MTHSK_INVARGMAT ; Error code
0000 83
0000 84 : EQUATED SYMBOLS:
0000 85
00000004 0000 86 value = 4 ; value.rg.r
0000 87
0000 88 :
0000 89 : MACROS: none
0000 90 :
0000 91 : PSECT DECLARATIONS:
0000 92
00000000 0000 93 .PSECT _MTH$CODE PIC,SHR,LONG,EXE,NOWRT
0000 94 ; program section for math routines
0000 95 :
0000 96 : OWN STORAGE: none
0000 97 :
0000 98 :
0000 99 : CONSTANTS:
0000 100 :
0000 101
2D18 5444 21FB 4019 0000 102 G_PI_OVER_2:
0008 103 .WORD ^0040031, ^0020773, ^0052104, ^0026430
0008 104 ; PI/2
2D18 5444 21FB 4029 0008 105 G_PI:
0010 106 .WORD ^0040051, ^0020773, ^0052104, ^0026430
0010 107 ; PI
00000000 80004076 0010 108 G_90:
0018 109 .LONG ^X80004076, ^X0 ; 90
00000000 80004086 0018 110 G_180:
0018 111 .LONG ^X80004086, ^X0 ; 180
```

```

0020 113          .SBTTL MTH$GACOS - Standard G Floating GACOS
0020 114
0020 115
0020 116 :++
0020 117 : FUNCTIONAL DESCRIPTION:
0020 118 :
0020 119 : GACOS - G floating point function
0020 120 :
0020 121 : GACOS(X) is computed as:
0020 122 :
0020 123 :     If X = 0, then GACOS(X) = PI/2.
0020 124 :     If X = 1, then GACOS(X) = 0.
0020 125 :     If X = -1, then GACOS(X) = PI.
0020 126 :     If 0 < X < 1/2, then GACOS(X) = ATAN(SQRT(1-X**2)/X).
0020 127 :     If 1/2 <= X < 1, then GACOS(X) = ATAN(SQRT((1-X)*(1+X))/X).
0020 128 :     If -1/2 < X < 0, then GACOS(X) = ATAN(SQRT(1-X**2)/X) + PI.
0020 129 :     If -1 < X <= -1/2, then GACOS(X) = ATAN(SQRT((1-X)*(1+X))/X) + PI
0020 130 :     If 1 < |X|, error.
0020 131 :
0020 132 : CALLING SEQUENCE:
0020 133 :
0020 134 :     gacos.wg.v = MTH$GACOS(x.rg.r)
0020 135 :
0020 136 : INPUT PARAMETERS:
0020 137 :
00000004 0020 138 :     LONG = 4 ; define longword multiplier
00000004 0020 139 :     x = 1 * LONG ; Contents of x is the argument
0020 140 :
0020 141 : IMPLICIT INPUTS: none
0020 142 :
0020 143 : OUTPUT PARAMETERS:
0020 144 :
0020 145 :     VALUE: G floating arc-cosine of the argument
0020 146 :
0020 147 : IMPLICIT OUTPUTS: none
0020 148 :
0020 149 : COMPLETION CODES: none
0020 150 :
0020 151 : SIDE EFFECTS:
0020 152 :
0020 153 : Signals: MTH$_INVARGMAT if |X| > 1 with reserved operand in R0/R1 (copied
0020 154 : to the signal_mechanism vector CHF$MCH_R0/R1 by LIB$SIGNAL).
0020 155 : Associated message is: "INVALID ARGUMENT". Result is reserved operand -0.0
0020 156 : unless a user supplied (or any) error handler changes CHF$MCH_R0/R1.
0020 157 :
0020 158 : NOTE: This procedure disables floating point underflow, enables integer
0020 159 : overflow.
0020 160 :
0020 161 : ---
0020 162 :
0020 163 :
0020 164 : .ENTRY MTH$GACOS, ^M<IV, R2, R3, R4, R5, R6, R7>
0022 165 : ; standard call-by-reference entry
0022 166 : ; disable DV (and FU), enable IV
0022 167 : MTH$FLAG_JACKET ; flag that this is a jacket procedure in
0022
6D 00000000'GF 9E 0022 MOVAB G^MTH$$JACKET_HND, (FP)

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0031 176      .SBTTL MTH$GACOS_R7 - Special GACOS routine
0031 177
0031 178      ; Special GACOS - used by the standard routine and direct JSB call.
0031 179
0031 180      ; CALLING SEQUENCE:
0031 181      ;   save anything needed in R0:R7
0031 182      ;   MOVG      R0                ; input in R0/R1
0031 183      ;   JSB      MTH$GACOS_R7
0031 184      ;   RSB
0031 185      ;
0031 186
0031 187      MTH$GACOS_R7::                ; special GACOS routine
0031 188      MTH$GACOS_R9::                ; Release 1 name
0031 189      MOVG      R0, R6              ; save X in R6/R7
56  50 50FD 0035 190      BNEQ      TEST_FOR_1.0 ; branch if !X! > 0
      05 12
0037 191
0037 192
0037 193      ; X = 0
0037 194
0037 195
50  C6 AF 7D 0037 196      MOVQ      G_PI_OVER_2, R0 ; R0/R1 = PI/2
      05 05 003B 197      RSB                ; return PI/2 if !X! = 0
003C 198
003C 199
003C 200      ; 0 < !X!
003C 201
003C 202
003C 203      TEST_FOR_1.0:
50  8000 8F AA 003C 204      BICW      #^X8000, R0 ; R0/R1 = !X!
      08 50 51FD 0041 205      CMPG      R0, #1 ; compare !X! with 1.0
      36 18 0045 206      BGEQ      GEQ_TO_1.0 ; branch if !X! >= 1.0
0047 207
0047 208
0047 209      ; 0 < !X! < 1.0
0047 210
0047 211
50  4000 8F B1 0047 212      CMPW      #^X4000, R0 ; Check for possible loss of
      0F 14 004C 213      BGTR      1$ ; significance
52  08 50 43FD 004E 214      SUBG3     R0, #1, R2 ; R2/R3 = 1 - X
      50 08 40FD 0053 215      ADDG2     #1, R0 ; R0/R1 = 1 + X
      50 52 44FD 0057 216      MULG2     R2, R0 ; R0/R1 = 1 - X^2
      09 11 005B 217      BRB      2$ ; Join main flow
50  50 50 44FD 005D 218 1$:  MULG2     R0, R0 ; R0/R1 = X**2
      08 50 43FD 0061 219      SUBG3     R0, #1, R0 ; R0/R1 = 1.0 - X**2
00000000'GF 16 0066 220 2$:  JSB      G^MTH$GSQRT_R5 ; R0/R1 = GSQRT(1-X**2)
      50 56 46FD 006C 221      DIVG2     R6, R0 ; R0/R1 = GSQRT(1-X**2)/X
      56 DD 0070 222      PUSHL     R6 ; save sign of X for sign test
00000000'GF 16 0072 223      JSB      G^MTH$GATAN_R7 ; R0/R1 = GATAN(GSQRT(1-X**2)/X)
      56 8E D0 0078 224      MOVL     (SP)+, R6 ; restore sign of X
      04 11 007B 225      BRB      TEST_SIGN ; branch to TEST_SIGN
007D 226
007D 227
007D 228      ; 1 <= !X!
007D 229
007D 230
007D 231      GEQ_TO_1.0:
      OE 14 007D 232      BGTR      ERROR ; branch to ERROR if !X! > 1.0

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007F 233
007F 234
007F 235
007F 236 : |X| = 1.0
007F 237 :
50 7C 007F 238
007F 239 CLRQ R0 ; R0/R1 = 0
0081 240
0081 241
0081 242 :
0081 243 : Test the sign of X in order to decide if add PI to the result
0081 244 :
0081 245
0081 246 TEST_SIGN:
56 53FD 0081 247 TSTG R6 ; test the sign of X
06 18 0084 248 BGEQ 10$ ; branch if X > 0
50 FF7D CF 40FD 0086 249 ADDG2 G_PI, R0 ; add PI to R0/R1 if X < 0
05 008C 250 10$: RSB ; return with result in R0/R1
008D 251
008D 252 :
008D 253 : 1 < |X|, error
008D 254 :
008D 255
7E 00'8F DD 008D 256 ERROR: PUSHL (SP) ; return PC from JSB routine
50 01 0F 79 008F 257 MOVZBL #MTH$K_INVARGMAT, -(SP) ; condition value
0093 258 ASHQ #15, #T, R0 ; R0 = result = reserved operand -0.0
0097 259 ; goes to signal mechanism vector
0097 260 ; (CHF$L_MCH_R0/R1) so error handler
0097 261 ; can modify the result.
00000000'GF 02 FB 0097 262 CALLS #2, G^MTH$$$SIGNAL ; signal error and use real user's PC
009E 263 ; independent of CALL vs JSB
05 009E 264 RSB ; return - R0 restored from CHF$L_MCH_R0/R1
009F 265

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```

009F 267          .SBTTL MTH$GACOSD - Standard G Floating GACOSD
009F 268
009F 269
009F 270 :++
009F 271 : FUNCTIONAL DESCRIPTION:
009F 272 :
009F 273 : GACOSD - G floating point function
009F 274 :
009F 275 : GACOSD(X) is computed as:
009F 276 :
009F 277 :     If X = 0, then GACOSD(X) = 90.
009F 278 :     If X = 1, then GACOSD(X) = 0.
009F 279 :     If X = -1, then GACOSD(X) = 180.
009F 280 :     If 0 < X < 1, then GACOSD(X) = GATAND(SQRT(1-X**2)/X).
009F 281 :     If 1/2 =< X < 1, then GACOS(X) = GATAND(SQRT((1-X)*(1+X))/X).
009F 282 :     If -1 < X < 0, then GACOSD(X) = GATAND(SQRT(1-X**2)/X) + 180.
009F 283 :     If -1 < X =< -1/2, then GACOS(X) = GATAND(SQRT((1-X)*(1+X))/X) + 180.
009F 284 :     If 1 < |X|, error.
009F 285 :
009F 286 : CALLING SEQUENCE:
009F 287 :
009F 288 :     GACOSD.wg.v = MTH$GACOSD(x.rg.r)
009F 289 :
009F 290 : INPUT PARAMETERS:
009F 291 :
009F 292 :     LONG = 4                ; define longword multiplier
00000004 009F 293 :     x = 1 * LONG           ; Contents of x is the argument
00000004 009F 294 :
009F 295 : IMPLICIT INPUTS:      none
009F 296 :
009F 297 : OUTPUT PARAMETERS:
009F 298 :
009F 299 :     VALUE: G floating arc-cosine of the argument
009F 300 :
009F 301 : IMPLICIT OUTPUTS:    none
009F 302 :
009F 303 : COMPLETION CODES:    none
009F 304 :
009F 305 : SIDE EFFECTS:
009F 306 :
009F 307 : Signals: MTH$_INVARGMAT if |X| > 1 with reserved operand in R0/R1 (co180ed
009F 308 : to the signal mechanism vector CHF$MCH_R0/R1 by LIB$SIGNAL).
009F 309 : Associated message is: "INVALID ARGUMENT". Result is reserved operand -0.0
009F 310 : unless a user supplied (or any) error handler changes CHF$_MCH_R0/R1.
009F 311 :
009F 312 : NOTE: This procedure disables floating point underflow, enables integer
009F 313 : overflow.
009F 314 :
009F 315 : ---
009F 316 :
009F 317 :
40FC 009F 318 : .ENTRY MTH$GACOSD, ^M<IV, R2, R3, R4, R5, R6, R7>
00A1 319 :     ; standard call-by-reference entry
00A1 320 :     ; disable DV (and FU), enable IV
00A1 321 :     MTH$FLAG_JACKET      ; flag that this is a jacket procedure in
6D 00000000'GF 9E 00A1 321 :     MOVAB G^MTH$$JACKET_HND, (FP)

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```

00B0 330      .SBTTL MTH$GACOSD_R7 - Special GACOSD routine
00B0 331
00B0 332      : Special GACOSD - used by the standard routine and direct JSB call.
00B0 333      :
00B0 334      : CALLING SEQUENCE:
00B0 335      :   save anything needed in R0:R7
00B0 336      :   MOVG      R0                ; input in R0/R1
00B0 337      :   JSB      MTH$GACOSD_R7
00B0 338      :   RSB                ; return with result in R0/R1
00B0 339      :
00B0 340
00B0 341 MTH$GACOSD_R7::
00B0 342      : special GACOSD routine
56 50 50FD 00B0 343      MOVG      R0, R6                ; save X in R6/R7
00B0 344      BNEQ     D_TEST_FOR_1.0        ; branch if |X| > 0
00B0 345      :
00B0 346      : X = 0
00B0 347      :
00B0 348
50 FF56 CF 7D 00B0 349      MOVQ     G_90, R0                ; R0/R1 = 90
00BB 350      RSB                ; return 90 if |X| = 0
00BC 351      :
00BC 352      : 0 < |X|
00BC 353      :
00BC 354      :
00BC 355
00BC 356 D_TEST_FOR_1.0:
50 8000 8F AA 00BC 357      BICW     #^X8000, R0                ; R0/R1 = |X|
00C1 358      CMPL     R0, #1                ; compare |X| with 1.0
00C5 359      BGEQ     D_GEQ_TO_1.0        ; branch if |X| >= 1.0
00C7 360      :
00C7 361      : 0 < |X| < 1.0
00C7 362      :
00C7 363      :
00C7 364
50 4000 8F B1 00C7 365      CMPW     #^X4000, R0                ; Check for possible loss of
00CC 366      BGTR     1$                    ; significance
52 08 50 43FD 00CE 367      SUBG3     R0, #1, R2                ; R2/R3 = 1 - X
00D3 368      ADDG2     #1, R0                ; R0/R1 = 1 + X
00D7 369      MULG2     R2, R0                ; R0/R1 = 1 - X^2
00DB 370      BRB                ; Join main flow
50 50 50 44FD 00DD 371 1$:      MULG2     R0, R0                ; R0/R1 = X**2
00E1 372      SUBG3     R0, #1, R0                ; R0/R1 = 1.0 - X**2
00000000'GF 16 00E6 373 2$:      JSB      G^MTH$GSQRT_R5        ; R0/R1 = GSQRT(1-X**2)
0050 56 46FD 00EC 374      DIVG2     R6, R0                ; R0/R1 = GSQRT(1-X**2)/X
00F0 375      PUSHL     R6                    ; save sign of X for sign test
00000000'GF 16 00F2 376      JSB      G^MTH$GATAND_R7        ; R0/R1 = GATAND(GSQRT(1-X**2)/X)
0056 8E D0 00F8 377      MOVL     (SP)+, R6                ; restore sign of X
00FB 378      BRB      D_TEST_SIGN            ; branch to D_TEST_SIGN
00FD 379      :
00FD 380      : 1 <= |X|
00FD 381      :
00FD 382      :
00FD 383
00FD 384 D_GEQ_TO_1.0:
00FD 385      BEQL     10$ ERROR                ; branch to ERROR if |X| > 1.0
FF8B 31 00FF 386      BRW

```

```
0102 387  
0103 388  
0104 389  
0105 390 : :X: = 1.0  
0106 391 : :  
0107 392 : :  
50 7C 0108 393 10$: CLRQ R0 ; R0/R1 = 0  
0109 394  
0110 395  
0111 396 : :  
0112 397 : : Test the sign of X in order to decide if add 180 to the result  
0113 398 : :  
0114 399 : :  
0115 400 D_TEST_SIGN:  
56 53FD 0116 401 TSTG R6 ; test the sign of X  
06 18 0117 402 BGEQ 10$ ; branch if X > 0  
50 FFOA CF 40FD 0118 403 ADDG2 G_180, R0 ; add 180 to R0/R1 if X < 0  
05 0119 404 10$: RSB ; return with result in R0/R1  
0120 405  
0121 406  
0122 407  
0123 408  
0124 409 .END
```

```

D_GEQ TO 1.0      000000FD R    01
D_TEST FOR 1.0   000000BC R    01
D_TEST_SIGN      00000104 R    01
ERROR            0000008D R    01
GEQ TO 1.0       0000007D R    01
G_180            00000018 R    01
G_90             00000010 R    01
G_PI             00000008 R    01
G_PI_OVER_2      00000000 R    01
LONG =           00000004
MTH$$JACKET_HND ***** X    01
MTH$$SIGNAL ***** X    00
MTH$GACOS        00000020 RG   01
MTH$GACOSD       0000009F RG   01
MTH$GACOSD R7    000000B0 RG   01
MTH$GACOS R7     00000031 RG   01
MTH$GACOS R9     00000031 RG   01
MTH$GATAN R7     ***** X    00
MTH$GATAN R7     ***** X    00
MTH$GSQRT R5     ***** X    00
MTH$K_INVARGMAT ***** X    00
TEST FOR 1.0     0000003C R    01
TEST_SIGN        00000081 R    01
VALUE =          00000004
    
```

 ! Psect synopsis !

| PSECT name | Allocation | PSECT No. | Attributes | | | | | | | | | | | |
|------------|------------------|-----------|------------|-----|-----|-----|-------|-------|------|-------|-------|------|--|--|
| ABS | 00000000 (0.) | 00 (0.) | NOPIC USR | CON | ABS | LCL | NOSHR | NOEXE | NORD | NOWRT | NOVEC | BYTE | | |
| _MTH\$CODE | 00000110 (272.) | 01 (1.) | PIC USR | CON | RE | LCL | SHR | EXE | RD | NOWRT | NOVEC | LONG | | |

 ! Performance indicators !

| Phase | Page faults | CPU Time | Elapsed Time |
|------------------------|-------------|-------------|--------------|
| Initialization | 33 | 00:00:00.11 | 00:00:00.63 |
| Command processing | 111 | 00:00:00.62 | 00:00:03.39 |
| Pass 1 | 92 | 00:00:01.16 | 00:00:03.64 |
| Symbol table sort | 0 | 00:00:00.01 | 00:00:00.01 |
| Pass 2 | 79 | 00:00:01.00 | 00:00:03.87 |
| Symbol table output | 4 | 00:00:00.03 | 00:00:00.03 |
| Psect synopsis output | 2 | 00:00:00.05 | 00:00:00.23 |
| Cross-reference output | 0 | 00:00:00.00 | 00:00:00.00 |
| Assembler run totals | 323 | 00:00:02.98 | 00:00:11.86 |

The working set limit was 1050 pages.
 6134 bytes (12 pages) of virtual memory were used to buffer the intermediate code.
 There were 10 pages of symbol table space allocated to hold 25 non-local and 7 local symbols.
 469 source lines were read in Pass 1, producing 14 object records in Pass 2.
 1 page of virtual memory was used to define 1 macro.

