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LL          II             SS
LL          II             SS
LL          II             SS
LL          II             SS
LL          II             SSSSSS
LL          II             SSSSSS
LL          II             SS
LL          II             SS
LL          II             SS
LL          II             SS
LLLLLLLLLLLL IIIIII          SSSSSSSS
LLLLLLLLLLLL IIIIII          SSSSSSSS

```


MTH\$DSQRT
Table of contents

H 16
; Double Floating Point Square Root rout 16-SEP-1984 01:22:02 VAX/VMS Macro V04-00

Page 0

(2) 55
(3) 85
(4) 126
(5) 207

HISTORY ; Detailed Current Edit History
DECLARATIONS ; Declarative Part of Module
MTH\$DSQRT - Standard Double Precision Floating DSQRT
MTH\$DSQRT_R5 - Special DSQRT routine

MTH\$DSQRT
1-015

I 16
; Double Floating Point Square Root rout 16-SEP-1984 01:22:02 VAX/VMS Macro V04-00 Page 1
6-SEP-1984 11:22:50 [MTHRTL.SRC]MTHDSQRT.MAR;1 (1)

```
0000 1      .TITLE  MTH$DSQRT      ; Double Floating Point Square Root routine
0000 2      ; (DSQRT)
0000 3      .IDENT  /1-015/        ; File: MTHDSQRT.MAR      EDIT:   RNH1015
0000 4      ;
0000 5      ;*****
0000 6      ;
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0000 24     ;
0000 25     ;*****
0000 26     ;
0000 27     ;
0000 28     ;
0000 29     ; FACILITY: MATH LIBRARY
0000 30     ; ++
0000 31     ; ABSTRACT:
0000 32     ;
0000 33     ; MTH$DSQRT is a function which returns the floating point square root
0000 34     ; of its single precision floating point argument. The call is standard
0000 35     ; call-by-reference.
0000 36     ; MTH$DSQRT_R5 is a special routine which is the same as MTH$DSQRT
0000 37     ; except a faster non-standard JSB call is used with the argument in
0000 38     ; R0 and no registers are saved.
0000 39     ;
0000 40     ; --
0000 41     ;
0000 42     ; VERSION: 01
0000 43     ;
0000 44     ; HISTORY:
0000 45     ; AUTHOR:
0000 46     ;      Peter Yuo, 15-Oct-76: Version 01
0000 47     ;
0000 48     ; MODIFIED BY:
0000 49     ;
0000 50     ; 01-1 Peter Yuo, 22-May-77
0000 51     ; 01-2 Peter Yuo, 31-May-77
0000 52     ;
0000 53     ;
```



```
0000 55      .SBTTL HISTORY ; Detailed Current Edit History
0000 56
0000 57
0000 58 : ALGORITHMIC DIFFERENCES FROM FP-11/C ROUTINE:
0000 59 : 1. Last DIVD is rounded instead of truncated. Results should be
0000 60 : correct within 2 LSB's.
0000 61 :
0000 62 : Edit History for Version 01 of MTH$DSQRT
0000 63 :
0000 64 : 01-1 Code saving after code review March 1977
0000 65 : 01-2 ROTL shift in garbage into highest bit. Use ASHL instead.
0000 66 : ADDL instruction after ADJUST has been changed into ADDW to prevent
0000 67 : overflow if R1<31:16> = FFFF and R0<31:16> = FFFF
0000 68 :
0000 69 : 01-3 Finish error handling 10-June-1977
0000 70 : 0-4 MTH$$ERROR changed to MTH$$SIGNAL.
0000 71 : MTH$ ... changed to MTH
0000 72 : Changed error handling mechanism. Put error result in R0:R1 before
0000 73 : calling MTH$$SIGNAL in order to allow user modify error result.
0000 74 : 01-5 - Return -0.0 on negative arg. TNH 20-Dec-77
0000 75 : 01-6 - Remove undefined $15 global. TNH 20-Dec-77
0000 76 : 01-7 - Add Rich Lary's code bums. JMT 26-Jan-78
0000 77 : 01-9 - Move .ENTRY symbol definition to module header. TNH 14-Aug-78
0000 78 : 1-010 - Update version number and copyright notice. JBS 16-NOV-78
0000 79 : 1-011 - Change symbol MTH_SQUROONEG to MTH$K_SQUROONEG. JBS 07-DEC-78
0000 80 : 1-012 - Add " to the PSECT directive. JBS 22-DEC-78
0000 81 : 1-013 - Declare externals. SBL 17-May-1979
0000 82 : 1-014 - Use ASHQ, not ASHL, to generate reserved operand. JAW 12-Oct-1979
0000 83 : 1-015 - Changed W^ to G^ in call to MTH$$SIGNAL RNH 09-Sept-1981
```

```

0000 85      .SBTTL  DECLARATIONS      ; Declarative Part of Module
0000 86
0000 87 :
0000 88 : INCLUDE FILES:      MTHJACKET.MAR
0000 89 :
0000 90
0000 91 :
0000 92 : EXTERNAL SYMBOLS:
0000 93 :
0000 94      .DSABL  GBL
0000 95      .EXTRN  MTH$K_SQUROONEG
0000 96      .EXTRN  MTH$$SIGNAL      ; SIGNAL SEVERE error
0000 97
0000 98 :
0000 99 : EQUATED SYMBOLS:
0000 100 :
0000 101
0000 102      ACMASK = ^M<IV, R2, R3, R4, R5> ; register save mask and IV enable
0000 103 :
0000 104 : MACROS:      none
0000 105 :
0000 106 : PSECT DECLARATIONS:
0000 107
0000 108      .PSECT  _MTH$CODE      PIC,SHR,LONG,EXE,NOWRT
0000 109      ; program section for math routines
0000 110 :
0000 111 : OWN STORAGE:  none
0000 112 :
0000 113 : CONSTANTS:
0000 114 :
0000 115 :
0000 116 : Constants A and B chosen for k = odd
0000 117 :
0000 118      LF_ODD_A_E63   =      ^X13CD5FD4
0000 119      LF_ODD_B_EM63 =      ^X3C4A2018
0000 120 :
0000 121 : Constants A and B chosen for k = even
0000 122 :
0000 123      LF_EVEN_A     =      ^XF61A4015
0000 124      LF_EVEN_B_EM64 =      ^X4B231FD7

```



```
0000 126 .SBTTL MTH$DSQRT - Standard Double Precision Floating DSQRT
0000 127
0000 128
0000 129 :++
0000 130 : FUNCTIONAL DESCRIPTION:
0000 131 :
0000 132 : DSQRT - double precision floating point function
0000 133 :
0000 134 : DSQRT(X) is computed using the following approximation technique:
0000 135 :
0000 136 : If X <= 0 , error. Let X = !X!.
0000 137 :
0000 138 : Let X = 2**K * F where F is the fractional part.
0000 139 :
0000 140 : If K = even, X = 2**(2P) * F,
0000 141 : DSQRT(X) = 2**P * DSQRT(F), 1/2 <= F < 1
0000 142 :
0000 143 : If K = odd, X = 2**(2P+1) * F = 2**(2P+2) * (F/2),
0000 144 : DSQRT(X) = 2**(P+1) * DSQRT(F/2), 1/4 <= F/2 < 1/2.
0000 145 :
0000 146 : Let F' = A*F + B,
0000 147 : A = 0.453730314(octal),
0000 148 : B = 0.327226214(octal), for K = even.
0000 149 : = A*(F/2) + B,
0000 150 : A = 0.650117146(octal),
0000 151 : B = 0.230170444(octal), for K = odd.
0000 152 :
0000 153 : and
0000 154 : K' = P, for K = even
0000 155 : = P + 1 for K = odd.
0000 156 :
0000 157 : Let Y0 = 2**K' * F' as a straight line approximation within the
0000 158 : given interval using coefficients A and B which minimize the
0000 159 : absolute error at the midpoint and endpoint.
0000 160 :
0000 161 : Starting with Y0, three Newton-Raphson iterations are performed.
0000 162 :
0000 163 : Y[n+1] = (1/2) * ( Y[n] + X/Y[n] )
0000 164 :
0000 165 : The relative error is < 10**-17.
0000 166 :
0000 167 : CALLING SEQUENCE:
0000 168 :
0000 169 : dsqrt.wd.v = MTH$DSQRT(x.rd.r)
0000 170 :
0000 171 : INPUT PARAMETERS:
0000 172 :
0000 173 : LONG = 4 ; define longword multiplier
0000 174 : x = 1 * LONG ; Contents of x is the argument
0000 175 :
0000 176 : IMPLICIT INPUTS: none
0000 177 :
0000 178 : OUTPUT PARAMETERS:
0000 179 :
0000 180 : VALUE: double precision square root of the argument
0000 181 :
0000 182 : IMPLICIT OUTPUTS: none
0000 183 :
```

00000004
00000004

MTH\$DSQRT
1-015

M 16
; Double Floating Point Square Root rout 16-SEP-1984 01:22:02 VAX/VMS Macro V04-00 Page 5
MTH\$DSQRT - Standard Double Precision F 6-SEP-1984 11:22:50 [MTHRTL.SRC]MTHDSQRT.MAR;1 (4)

```
0000 183 : COMPLETION CODES: none
0000 184 :
0000 185 : SIDE EFFECTS:
0000 186 :
0000 187 : Signals: MTH$_SQUROONEG if X < 0.0 with reserved operand in R0/R1
0000 188 : (copied to the signal mechanism vector CHF$$_MCH_R0/R1 by LIB$$_SIGNAL).
0000 189 : Associated message is: "SQUARE ROOT OF NEGATIVE VALUE". Result is reserved
0000 190 : operand -0.0 unless a user supplied (or any) error handler changes CHF$$_MCH_R0/R1
0000 191 :
0000 192 : NOTE: This procedure disables floating point underflow, enables integer
0000 193 : overflow, causes no floating overflow or other arithmetic traps, and
0000 194 : preserves enables across the call.
0000 195 :
0000 196 : ---
0000 197 :
403C 0000 198
0002 200 .ENTRY MTH$DSQRT, ACMASK ; standard call-by-reference entry
0002 201 MTH$FLAG_JACKET ; disable DV (and FU), enable IV
; flag that this is a jacket procedure in
6D 00000000'GF 9E 0002 MOVAB G^MTH$$_JACKET_HND, (FP)
; set handler address to jacket
0009 ; handler
0009
50 04 BC 70 0009 202 ; case of an error in special routine
01 10 000D 203 ; R0/R1 = arg
04 000F 204 ; call kernel DSQRT routine
205 RET ; return - result in R0/R1
```



```
0010 207 .SBTTL MTH$DSQRT_R5 - Special DSQRT routine
0010 208
0010 209 ; Special DSQRT - used by the standard routine, and directly.
0010 210
0010 211 ; CALLING SEQUENCE:
0010 212 ; save anything in R2:R5
0010 213 ; MOVD R0 ; input in R0/R1
0010 214 ; JSB MTH$DSQRT_R5
0010 215 ; return with result in R0/R1
0010 216 ; Note: This routine is written to avoid causing any integer overflows, floating
0010 217 ; overflows, floating underflows or divide by 0 conditions, whether enabled or
0010 218 ; not.
0010 219
0010 220 ; REGISTERS USED:
0010 221 ; R0/R1 - Floating argument then result
0010 222 ; R2/R3 - scratch
0010 223 ; R4/R5 - hold X during calc of F', K'.
0010 224
0010 225 MTH$DSQRT_R5::
0010 226 MOVD R0, R4 ; JSB routine for DSQRT
54 50 70 0010 227 BLEQ ZERO_NEG ; test sign of X and save it in R4/R5.
5D 15 0013 228 ; branch to ZERO_NEG if X <= 0
0015 229 ;
0015 230 ; X > 0
0015 231 POS: MOVZWL R0, R1 ; isolate low 16 bits (sign,exp,>fract) in R
51 50 3C 0015 232 CLRB R1 ; R1 now has sign and left 7 exp bits
51 94 0018 233 BICW R1, R0 ; clear sign and left 7 exp bits
50 51 AA 001A 234 TSTB R0 ; check low bit of exp
50 50 95 001D 235 BGEQ EVEN ; and branch if 1
10 18 001F 236 MULF #LF_ODD_A_E63, R0 ; add 64 (half of bias) to (exponent-2)
50 13CD5FD4 8F 44 0021 237 ; and start approximation calc
0028 238 ADDF #LF_ODD_B_EM63, R0 ; R0 = (first approx) * 2**-64
50 3C4A2018 8F 40 0028 239 BRB ADJUST ; go adjust
13 11 002F 240
0031 241 EVEN:
0031 242 ADDW #X2000, R0 ; exp is 0 - make it 64 (2**-64) for legalit
50 2000 8F A0 0031 243 MULF #LF_EVEN_A, R0
50 F61A4015 8F 44 0036 244 ADDF #LF_EVEN_B_EM64, R0 ; R0 = (first approx) * 2**-64
50 4B231FD7 8F 40 003D 245 ADJUST:
0044 246 ROTL #31, R1, R1 ; divide R1 (exp+bias) by 2,
51 51 1F 9C 0044 247 ; giving (exp/2+64)
0048 248 ADDW R1, R0 ; insert exp/2 in first approx and
50 51 A0 0048 249 ; re-bias it.
004B 250
004B 251 ; first iteration - single precision is sufficient
004B 252 ;
51 54 50 47 004B 253 DIVF3 R0, R4, R1 ; R1 = X/Y0
50 50 51 40 004F 254 ADDF R1, R0 ; R0 = Y0 + X/Y0
50 0080 8F A2 0052 255 SUBW #X80, R0 ; R0 = Y1 = (1/2)(Y0 + X/Y0)
0057 256 ; no overflow possible
0057 257
0057 258 ; second iteration, do in double precision to get truncated( rather than
0057 259 ; rounded) result.
0057 260 ;
52 54 51 D4 0057 261 CLRL R1 ; lower part (X) = 0
50 50 52 67 0059 262 DIVD3 R0, R4, R2 ; R2/R3 = X/Y1
50 50 52 60 005D 263 ADDD R2, R0 ; R0/R1 = Y1 + higher_part(X/Y1)
```

```
50 0080 8F A2 0060 264 SUBW #^X80, R0 ; R0/R1 = Y2 = (1/2) (Y1+X/Y1)
; third iteration, do in double precision.
52 54 50 67 0065 265
50 50 52 60 0065 266
50 0080 8F A2 0065 267
0065 268
0069 269
006C 270
0071 271
05 0071 272 SQRX: RSB
0072 273
0072 274 ; X =< 0
0072 275
0072 276 ZERO_NEG:
FD 13 0072 277 BEQL SQRX ; return with R0 = result = 0
6E DD 0074 278 PUSHL (SP) ; return PC from JSB routine
7E 00 8F 9A 0076 279 MOVZBL #MTH$K_SQUROONEG, -(SP) ; condition value
50 01 0F 79 007A 280 ASHQ #15, #T, R0 ; R0/R1 = result = reserved operand -0.0
; R0/R1 goes to signal mechanism vector
; (CHF$MCH_R0/R1) so error handler
; can modify the result.
00000000'GF 02 FB 007E 281 CALLS #2, G^MTH$$SIGNAL ; signal error and use real user's PC
0085 282 ; independent of CALL vs JSB
05 0085 283 ; return - R0 restored from CHF$MCH_R0/R1
0086 284
0086 285
0086 286
0086 287
0086 288 .END
```


MTH\$DSQRT
Symbol table

D 1
; Double Floating Point Square Root rout 16-SEP-1984 01:22:02 VAX/VMS Macro V04-00
6-SEP-1984 11:22:50 [MTHRTL.SRC]MTHDSQRT.MAR;1

Page 8
(5)

ACMASK = 0000403C
ADJUST 00000044 R 01
EVEN 00000031 R 01
LF_EVEN_A = F61A4015
LF_EVEN_B_EM64 = 4B231FD7
LF_ODD_A_E63 = 13CD5FD4
LF_ODD_B_EM63 = 3C4A2018
LONG = 00000004
MTH\$\$JACKET_HND ***** X 01
MTH\$\$SIGNAL ***** X 00
MTH\$DSQRT 00000000 RG 01
MTH\$DSQRT_R5 00000010 RG 01
MTH\$K_SQUROONEG ***** X 00
POS 00000015 R 01
SQRX 00000071 R 01
X = 00000004
ZERO_NEG 00000072 R 01

+-----+
! Psect synopsis !
+-----+

PSECT name	Allocation	PSECT No.	Attributes														
ABS	00000000 (0.)	00 (0.)	NOPIC	USR	CON	ABS	LCL	NOSHR	NOEXE	NORD	NOWRT	NOVEC	BYTE				
MTH\$CODE	00000086 (134.)	01 (1.)	PIC	USR	CON	REL	LCL	SHR	EXE	RD	NOWRT	NOVEC	LONG				

+-----+
! Performance indicators !
+-----+

Phase	Page faults	CPU Time	Elapsed Time
Initialization	29	00:00:00.08	00:00:01.27
Command processing	106	00:00:00.63	00:00:05.92
Pass 1	82	00:00:00.88	00:00:04.28
Symbol table sort	0	00:00:00.01	00:00:00.01
Pass 2	64	00:00:00.68	00:00:03.11
Symbol table output	3	00:00:00.04	00:00:00.16
Psect synopsis output	2	00:00:00.01	00:00:00.02
Cross-reference output	0	00:00:00.00	00:00:00.00
Assembler run totals	288	00:00:02.33	00:00:14.77

The working set limit was 900 pages.
4182 bytes (9 pages) of virtual memory were used to buffer the intermediate code.
There were 10 pages of symbol table space allocated to hold 17 non-local and 0 local symbols.
348 source lines were read in Pass 1, producing 11 object records in Pass 2.
1 page of virtual memory was used to define 1 macro.

+-----+
! Macro library statistics !
+-----+

Macro library name	Macros defined
_\$255\$DUA28:[SYSLIB]STARLET.MLB;2	0

MTH\$DSQRT ; Double Floating Point Square Root rout 16-SEP-1984 01:22:02 VAX/VMS Macro V04-00 Page 9
VAX-11 Macro Run Statistics 6-SEP-1984 11:22:50 [MTHRTL.SRC]MTHDSQRT.MAR;1 (5)

0 GETS were required to define 0 macros.

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL,TRACEBACK)/LIS=LIS\$:MTH\$DSQRT/OBJ=OBJ\$:MTHDSQRT MSRC\$:MTHJACKET/UPDATE=(ENH\$:MTHJACKET)+MSRC

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