


```

MM      MM      TTTTTTTTTT  HH      HH      DDDDDDDD  SSSSSSSS  IIIIII  NN      NN  HH      HH
MM      MM      TTTTTTTTTT  HH      HH      DDDDDDDD  SSSSSSSS  IIIIII  NN      NN  HH      HH
MMMM    MMMM    TT          HH      HH      DD      DD  SS          II      NN      NN  HH      HH
MMMM    MMMM    TT          HH      HH      DD      DD  SS          II      NN      NN  HH      HH
MM      MM      TT          HH      HH      DD      DD  SS          II      NNNN   NN  HH      HH
MM      MM      TT          HH      HH      DD      DD  SS          II      NNNN   NN  HH      HH
MM      MM      TT          HHHHHHHHHH  DD      DD  SSSSSS   II      NN  NN  NN  HHHHHHHHHH
MM      MM      TT          HHHHHHHHHH  DD      DD  SSSSSS   II      NN  NN  NN  HHHHHHHHHH
MM      MM      TT          HH      HH      DD      DD          SS      II      NN      NNNN  HH      HH
MM      MM      TT          HH      HH      DD      DD          SS      II      NN      NNNN  HH      HH
MM      MM      TT          HH      HH      DD      DD          SS      II      NN      NN  HH      HH
MM      MM      TT          HH      HH      DD      DD          SS      II      NN      NN  HH      HH
MM      MM      TT          HH      HH      DDDDDDDD  SSSSSSSS  IIIIII  NN      NN  HH      HH
MM      MM      TT          HH      HH      DDDDDDDD  SSSSSSSS  IIIIII  NN      NN  HH      HH

```

```

LL      IIIIII  SSSSSSSS
LL      IIIIII  SSSSSSSS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SSSSSS
LL      II      SSSSSS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SS
LLLLLLLLLLLL  IIIIII  SSSSSSSS
LLLLLLLLLLLL  IIIIII  SSSSSSSS

```

MTH\$DSINH
Table of contents

J 15
: Double Floating Hyperbolic Sine routin 16-SEP-1984 01:21:28 VAX/VMS Macro V04-00

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(2) 50
(3) 84
(4) 148

HISTORY ; Detailed Current Edit History
DECLARATIONS ; Declarative Part of Module
MTH\$DSINH - Standard Double Precision Floating DSINH

```
0000 1 .TITLE MTH$DSINH ; Double Floating Hyperbolic Sine routine
0000 2 ; (DSINH)
0000 3 .IDENT /1-008/ ; File: MTHDSINH.MAR Edit: RNH1008
0000 4 :
0000 5 :*****
0000 6 :*
0000 7 :* COPYRIGHT (c) 1978, 1980, 1982, 1984 BY
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0000 23 :* SOFTWARE ON EQUIPMENT WHICH IS NOT SUPPLIED BY DIGITAL.
0000 24 :*
0000 25 :*
0000 26 :*****
0000 27 :
0000 28 :
0000 29 : FACILITY: MATH LIBRARY
0000 30 :++
0000 31 : ABSTRACT:
0000 32 :
0000 33 : MTH$DSINH is a function which returns the double floating hyperbolic sine
0000 34 : of its double precision floating point argument. The call is standard
0000 35 : call-by-reference.
0000 36 :
0000 37 :--
0000 38 :
0000 39 : VERSION: 01
0000 40 :
0000 41 : HISTORY:
0000 42 : AUTHOR:
0000 43 : Peter Yuo, 29-Jun-77: Version 01
0000 44 :
0000 45 : MODIFIED BY:
0000 46 :
0000 47 :
0000 48 :
```

```

0000 50          .SBTTL HISTORY ; Detailed Current Edit History
0000 51
0000 52
0000 53 : ALGORITHMIC DIFFERENCES FROM FP-11/C ROUTINE: none
0000 54
0000 55 : Edit History for Version 01 of MTHSDSINH
0000 56
0000 57 : 0-2 MTH$ERROR changed to MTH$$SIGNAL.
0000 58 : MTH$... changed to MTH
0000 59 : Changed error handling mechanism. Put error result in R0:R1 before
0000 60 : calling MTH$$SIGNAL in order to allow user modify error result.
0000 61
0000 62 : 0-3 Six term Taylor series, in powers of argument, replaced
0000 63 : by six term Chebyshev series, in powers of ARG**2
0000 64 : with overhang provided. This improves accuracy. 18-May-1978;
0000 65 : Mary Payne.
0000 66 : 0-4 Fix LOG(2) constant. TNH 16-June-78
0000 67 : 1-001 - Update version number and copyright notice. JBS 16-NOV-78
0000 68 : 1-002 - Change MTH_FLOOVEMAT to MTH$K_FLOOVEMAT. JBS 07-DEC-78
0000 69 : 1-003 - Remove $$SRMDEF - not needed. JBS 16-DEC-78
0000 70 : 1-004 - Add "" to the PSECT directive. JBS 22-DEC-78
0000 71 : 1-005 - Declare externals. SBL 17-May-1979
0000 72 : 1-006 - Use MTH$DEXP R6. SBL 27-Sept-1979
0000 73 : 1-007 - Changed lower limit for Chebyshev approximation from 2**-27 to
0000 74 : 2**-28.
0000 75 : - Eliminated second call to EXP for input values between 28.5*ln2
0000 76 : and 127*ln2.
0000 77 : - Changed all final floating point divisions by 2 to interger
0000 78 : subtracts of 1 from the exponent field.
0000 79 : - Extended maximum range from 87.69 to 128*ln2=88.72.
0000 80 : - Changed logic for computing EXP(|x|-ln2) to reduce error.
0000 81 : - RNH 10-FEB-81
0000 82 : 1-008 - Change W^ to G^ on call to MTH$$SIGNAL RNH 09-Sept-1981
  
```

```

0000 84      .SBTTL  DECLARATIONS      ; Declarative Part of Module
0000 85
0000 86      :
0000 87      : INCLUDE FILES:          MTHJACKET.MAR
0000 88      :
0000 89      :
0000 90      :
0000 91      : EXTERNAL SYMBOLS:
0000 92      :
0000 93      :     .DSABL  GBL
0000 94      :     .EXTRN  MTH$DEXP R6
0000 95      :     .EXTRN  MTH$K_FLOOVEMAT
0000 96      :     .EXTRN  MTH$$SIGNAL
0000 97
0000 98      :
0000 99      : EQUATED SYMBOLS:
0000 100
00004080 0000 101      SD 1.0 = ^F1.0          ; 1.0
00000004 0000 102      value = 4              ; value.rd.r
0000 103
0000 104      :
0000 105      : MACROS:          none
0000 106      :
0000 107      :
0000 108      : PSECT DECLARATIONS:
0000 109
00000000 0000 110      .PSECT  _MTH$CODE          PIC,SHR,LONG,EXE,NOWRT
0000 111      :                               ; program section for math routines
0000 112      :
0000 113      : OWN STORAGE:  none
0000 114      :
0000 115      :
0000 116      : CONSTANTS:
0000 117      :
0000 118      :
0000 119      D_127_LOG_2:
2BDAC7E2 0F3343B0 0000 120      .QUAD  ^X2BDAC7E20F3343B0      ; 127*ln2
0008 121      D_128_LOG_2:
CF78F7D1 721743B1 0008 122      .QUAD  ^XCF78F7D1721743B1      ; 128*ln2-2**+49
0010 123      D_28.5_LOG_2:
DCC858B6 0990429E 0010 124      .QUAD  ^XDCC858B60990429E      ; 28.5*ln2
0018 125      D_LOG_2_HI:
CF80F7D1 72174031 0018 126      .QUAD  ^XCF80F7D172174031      ; (high 49 bits of ln2)+2**+49
0020 127      D_LOG_2_LO:
FF81898C 86C3A5CA 0020 128      .QUAD  ^XFF81898C86C3A5CA      ; ln2 - D_LOG_2_HI
0028 129
0028 130      DSINHTAB:
0028 131
0028 132      .WORD  ^0031727,^0072153
746B 33D7 0028 133      .WORD  ^0121466,^0073017      ; DECIMAL:  0.2508223608819151D-07
760F A336 002C 134      .WORD  ^0033470,^0167423
EF13 3738 0030 135      .WORD  ^0154465,^0062340      ; DECIMAL:  0.2755729803646086D-05
64E0 D935 0034 136      .WORD  ^0035120,^0006400
0D00 3A50 0038 137      .WORD  ^0150502,^0041641      ; DECIMAL:  0.1984126984813681D-03
43A1 D142 003C 138      .WORD  ^0036410,^0104210
8888 3D08 0040 139      .WORD  ^0104210,^0073152      ; DECIMAL:  0.8333333333332327D-02
766A 8888 0044 140      .WORD  ^0037452,^0125252
AAAA 3F2A 0048

```



```

0058 148      .SBTTL MTH$DSINH - Standard Double Precision Floating DSINH
0058 149
0058 150
0058 151      :++
0058 152      : FUNCTIONAL DESCRIPTION:
0058 153      :
0058 154      : DSINH - double precision floating point function
0058 155      :
0058 156      : DSINH(X) is computed as:
0058 157      :
0058 158      :   If |X| < 2**(-28), DSINH(X) = X.
0058 159      :   If 2**(-28) =< |X| < 0.25, DSINH(X) = Chebyshev Series.
0058 160      :   If 0.25 =< |X| < 28.5*ln2, DSINH(X) = (DEXP(X) - DEXP(-X))/2.
0058 161      :   If 28.5 =< |X| < 127*ln2, DSINH(X) = sign(X)*EXP(|X|)/2.
0058 162      :   If 127*ln2 =< |X| < 128*ln2, then DSINH(X) = sign(X)*DEXP(X - ln2).
0058 163      :   If 128*ln2 < |X|, then overflow.
0058 164      :
0058 165      : CALLING SEQUENCE:
0058 166      :
0058 167      :   DSINH.wd.v = MTH$DSINH(x.rd.r)
0058 168      :
0058 169      : INPUT PARAMETERS:
0058 170      :
00000004 0058 171      :   LONG = 4 ; define longword multiplier
00000004 0058 172      :   x = 1 * LONG ; contents of x is the argument
0058 173      :
0058 174      : IMPLICIT INPUTS: none
0058 175      :
0058 176      : OUTPUT PARAMETERS:
0058 177      :
0058 178      :   VALUE: double precision floating hyperbolic sine of the argument
0058 179      :
0058 180      : IMPLICIT OUTPUTS: none
0058 181      :
0058 182      : COMPLETION CODES: none
0058 183      :
0058 184      : SIDE EFFECTS:
0058 185      :
0058 186      : Signal: MTH$ FLOOVEMAT if 128*ln2 =< |X| with reserved operand in R0/R1
0058 187      : (copied to the signal mechanism vector CHFSL_MCH_R0/R1 by LIB$SIGNAL).
0058 188      : Associated message is: "FLOATING OVERFLOW IN MATH LIBRARY". Result is reserved
0058 189      : operand -0.0 unless a user supplied (or any) error handler changes CHFSL_MCH_R0/R1
0058 190      :
0058 191      : NOTE: This procedure disables floating point underflow, enables integer
0058 192      : overflow.
0058 193      :
0058 194      : ---
0058 195      :
0058 196      :
0058 197      : .ENTRY MTH$DSINH, ^M<IV, R2, R3, R4, R5, R6, R7>
005A 198      : ; standard call-by-reference entry
005A 199      : ; disable DV (and FU), enable IV
005A 200      : MTH$FLAG_JACKET ; flag that this is a jacket procedure in
005A
6D 00000000'GF 9E 005A MOVAB G^MTH$$JACKET_HND, (FP) ; set handler address to jacket
0061 ; handler
0061

```

```

0061
0061 201 ; case of an error in routine
0061 202 ; If an error, convert signal to user PC
0061 203 ; and resignal
56 04 BC 70 0061 204 MOVD @value(AP), R6 ; R6/R7 = 'X' = @value(AP)
50 50 56 7D 0065 205 MOVQ R6, R0
50 8000 8F AA 0068 206 BICW2 #^X8000, R0 ; R0/R1 = 'X'
3F80 8F 50 B1 006D 207 CMPW R0, #^X3F80 ; compare 'X' with 0.25
1A 18 0072 208 BGEQ GEQ_TO_0.25 ; branch if 'X' >= 0.25
0074 209
0074 210 ;
0074 211 ; 'X' < 0.25
0074 212 ;
0074 213 ;
3280 8F 50 B1 0074 214 CMPW R0, #^X3280 ; compare 'X' with 2** -28
04 18 0079 215 BGEQ GEQ_TO_2M28 ; branch if 'X' >= 2** -28
007B 216
007B 217 ;
007B 218 ; 'X' < 2** -28
007B 219 ;
007B 220 ;
50 56 7D 007B 221 MOVQ R6, R0 ; R0/R1 = X
04 007E 222 RET ; return with result = argument
007F 223
007F 224 ;
007F 225 ; 2** -28 =< 'X' < 0.25
007F 226 ;
007F 227 ;
007F 228 GEQ_TO_2M28:
A1 AF 50 50 64 007F 229 MULD R0, R0 ; Get ARG**2 for POLYD
05 50 75 0082 230 POLYD R0, #DSINHLEN-1, DSINHTAB ;
0087 231 ; R0/R1 = SUM(Ci*X**i), with
0087 232 ; Last coefficient zero
50 56 64 0087 233 MULD R6, R0 ; MULD by ARG, and then
50 56 60 008A 234 ADDD R6, R0 ; Add in ARG with overhang.
04 008D 235 RET ; return with result in R0/R1
008E 236
008E 237 ;
008E 238 ; 0.25 =< 'X'
008E 239 ;
008E 240 ;
008E 241 GEQ_TO_0.25:
FF6D CF 50 71 008E 242 CMPD R0, D 127 LOG_2 ; compare 'X' with 127*ln2
3B 14 0093 243 BGTR GTR_TRAN_T27_LOG_2 ; branch if 'X' > 127*ln2
0095 244
0095 245 ;
0095 246 ; 0.25 =< 'X' < 127*ln2
0095 247 ;
0095 248 ;
FF76 CF 50 71 0095 249 CMPD R0, D 28.5 LOG_2 ; Compare 'X' with 28.5*ln2, if
20 14 009A 250 BGTR ONLY_ONE_TERM ; greater, only one of EXP(X) and
009C 251 ; EXP(-X) is significant.
009C 252 ;
009C 253 ; 0.25 =< 'X' < 28.5*ln2
009C 254 ;
50 56 7D 009C 255 MOVQ R6, R0 ; R0/R1 = X
00000000 EF 16 009F 256 JSB MTH$DEXP_R6 ; R0/R1 = DEXP(X)

```

```

    7E 50 7D 00A5 257      MOVQ   RO, -(SP)           ; push DEXP(X) on stack
    50 04 BC 72 00A8 258      MNEGD  @value(AP), RO      ; R0/R1 = -X
00000000'EF 16 0CAC 259      JSB    MTH$DEXP R6         ; R0/R1 = DEXP(-X)
    50 8E 50 63 00B2 260      SUBD3  RO, (SP)+, RO       ; R0/R1 = DEXP(X) - DEXP(-X)
    50 0080 8F A2 00B6 261      SUBW   #^X0080, RO        ; R0/R1 = (DEXP(X)-DEXP(-X))/2
    04 00BB 262      RET                               ; return with result in R0/R1
    00BC 263
    00BC 264      ; 28.5*ln2 =< |X| <127*ln2
    00BC 265
    00BC 266
    00BC 267
    00BC 268 ONLY_ONE_TERM:
    00000000'EF 16 00BC 269      JSB    MTH$DEXP R6         ; R0/R1 = DEXP(|X|)
    04 BC 73 00C2 270      TSTD  @value(AP)         ; Check sign of X
    03 14 00C5 271      BGTR  POSITIVE           ; If negative change sign of
    50 50 72 00C7 272      MNEGD RO, RO             ; DEXP(|X|)
    00CA 273 POSITIVE:
    50 0080 8F A2 00CA 274      SUBW   #^X0080, RO        ; R0/R1 = sign(X)*DEXP(|X|)/2
    04 00CF 275      RET
    00D0 276
    00D0 277      ; 127*ln2 < |X|
    00D0 278
    00D0 279
    00D0 280 GTR_THAN_127_LOG_2:
    FF33 CF 50 71 00D0 281      CMPD  RO, D_128_LOG_2    ; Compare |X| to 128*ln2
    1D 18 00D3 282      BGEQ  ERROR             ; if 128*ln2 =< |X|, overflow occurs
    00D7 283
    00D7 284
    00D7 285
    00D7 286      ; 127*ln2 < |X| < 128*ln2
    00D7 287
    00D7 288
    50 FF3D CF 62 00D7 289      SUBD  D_LOG_2_HI, RO     ; R0/R1=|X|-D_LOG_2_HI
    00000000'EF 16 00DC 290      JSB   MTH$DEXP R6         ; R0/R1 = DEXP(|X|-D_LOG_2_HI)
52 50 FF3A CF 65 00E2 291      MULD3 D_LOG_2_LO, RO, R2 ; R2/R3=DEXP(|X|-D_LOG_2_HI)*D_LOG_2_LO
    50 52 62 00E8 292      SUBD  R2, RO             ; R0/R1=DEXP(|X|-ln2)
    04 BC 73 00EB 293      TSTD  @value(AP)         ; test the sign of X
    03 18 00EE 294      BGEQ  10$               ; branch if X >= 0
    50 50 72 00F0 295      MNEGD RO, RO            ; R0/R1 = sign(X) * DEXP(|X|-ln2)
    04 00F3 296 10$: RET                               ; return with result in R0/R1
    00F4 297
    00F4 298
    00F4 299      ; 128*ln2 =< |X|, error
    00F4 300
    00F4 301
    7E 00'8F 9A 00F4 302 ERROR: MOVZBL #MTH$K_FLOOVEMAT, -(SP) ; condition value
    50 01 0F 79 00F8 303      ASHQ  #15, #T, RO        ; R0/R1 = result = reserved operand -0.0
    00FC 304
    00FC 305
    00FC 306
    00000000'GF 01 FB 00FC 307      CALLS #1, G^MTH$$SIGNAL ; signal error and use real user's PC
    0103 308
    04 0103 309      RET                               ; independent of CALL vs JSB
    0104 310
    0104 311
    0104 312
    0104 313      .END

```

```

DSINHLEN      = 00000006
DSINH7AB      = 00000028 R      01
D_127_LOG_2   = 00000000 R      01
D_128_LOG_2   = 00000008 R      01
D_28.5_LOG_2  = 00000010 R      01
D_LOG_2_HI    = 00000018 R      01
D_LOG_2_LO    = 00000020 R      01
ERROR         = 000000F4 R      01
GEQ_TO_0.25   = 0000008E R      01
GEQ_TO_2M28   = 0000007F R      01
GTR_THAN_127_LOG_2 = 000000D0 R      01
LONG          = 00000004
MTH$$JACKET_HND ***** X      01
MTH$$SIGNAL   ***** X      00
MTH$DEXP_R6   ***** X      00
MTHSDSINH     00000058 RG     01
MTH$K_FLOOVMAT ***** X      00
ONLY_ONE_TERM 000000BC R      01
POSITIVE      000000CA R      01
VALUE        = 00000004
    
```

+-----+
! Psect synopsis !
+-----+

PSECT name	Allocation	PSECT No.	Attributes													
ABS	00000000 (0.)	00 (0.)	NOPIC USR	CON	ABS	LCL	NOSHR	NOEXE	NORD	NOWRT	NOVEC	BYTE				
_MTH\$CODE	00000104 (260.)	01 (1.)	PIC USR	CON	REL	LCL	SHR	EXE	RD	NOWRT	NOVEC	LONG				

+-----+
! Performance indicators !
+-----+

Phase	Page faults	CPU Time	Elapsed Time
Initialization	35	00:00:00.12	00:00:01.77
Command processing	120	00:00:00.67	00:00:05.67
Pass 1	88	00:00:00.90	00:00:05.83
Symbol table sort	0	00:00:00.01	00:00:00.01
Pass 2	68	00:00:00.71	00:00:03.50
Symbol table output	4	00:00:00.03	00:00:00.03
Psect synopsis output	2	00:00:00.02	00:00:00.02
Cross-reference output	0	00:00:00.00	00:00:00.00
Assembler run totals	319	00:00:02.46	00:00:16.83

The working set limit was 900 pages.
 4682 bytes (10 pages) of virtual memory were used to buffer the intermediate code.
 There were 10 pages of symbol table space allocated to hold 22 non-local and 1 local symbols.
 373 source lines were read in Pass 1, producing 11 object records in Pass 2.
 1 page of virtual memory was used to define 1 macro.

↑-----↑
! Macro library statistics !
↑-----↑

Macro library name

Macros defined

_S255SDUA28:[SYSLIB]STARLET.MLB;2

0

0 GETS were required to define 0 macros.

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL,TRACEBACK)/LIS=LIS\$:MTHDSINH/OBJ=OBJ\$:MTHDSINH MSRCS:MTHJACKET/UPDATE=(ENHS:MTHJACKET)+MSRC

