


```

MM      MM      TTTTTTTTTT  HH      HH      DDDDDDDD  MM      MM      000000  DDDDDDDD
MM      MM      TTTTTTTTTT  HH      HH      DDDDDDDD  MM      MM      000000  DDDDDDDD
MMMM    MMMM      TT          HH      HH      DD          DD  MMMM    MMMM  00          00  DD          DD
MMMM    MMMM      TT          HH      HH      DD          DD  MMMM    MMMM  00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HHHHHHHHHH  DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HHHHHHHHHH  DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DD          DD  MM      MM      00          00  DD          DD
MM      MM      TT          HH      HH      DDDDDDDD  MM      MM      000000  DDDDDDDD
MM      MM      TT          HH      HH      DDDDDDDD  MM      MM      000000  DDDDDDDD

```

```

LL      IIIIII  SSSSSSSS
LL      IIIIII  SSSSSSSS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SS
LL      II      SSSSSS
LL      II      SSSSSS
LL      II      SS
LL      II      SS
LL      II      SS
LL      IIIIII  SSSSSSSS
LLLLLLLLLL  IIIIII  SSSSSSSS
LLLLLLLLLL  IIIIII  SSSSSSSS

```

(1)	49	HISTORY	; Detailed Current Edit History
(2)	54	DECLARATIONS	
(3)	89	MTHSDMOD - D REAL*8 remainder	

```

0000 1      .TITLE MTH$DMOD
0000 2      .IDENT /3-001/                ; File: MTHDMOD.MAR Edit: JCW3001
0000 3
0000 4
0000 5 :*****
0000 6 :*
0000 7 :*  COPYRIGHT (c) 1978, 1980, 1982, 1984 BY
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0000 22 :*  DIGITAL ASSUMES NO RESPONSIBILITY FOR THE USE OR RELIABILITY OF ITS
0000 23 :*  SOFTWARE ON EQUIPMENT WHICH IS NOT SUPPLIED BY DIGITAL.
0000 24 :*
0000 25 :*
0000 26 :*****
0000 27
0000 28
0000 29 :++
0000 30 : FACILITY: MATH LIBRARY
0000 31
0000 32 : ABSTRACT:
0000 33
0000 34 :   This module contains the routine MTH$DMOD:
0000 35 :   It returns the remainder of the division of arg1/arg2 using
0000 36 :   the following equation:
0000 37 :       arg1 - (int(arg1/arg2))*arg2
0000 38
0000 39
0000 40 :--
0000 41
0000 42 : AUTHOR: Jeffrey C. Wiener, CREATION DATE: 21-DEC-1982
0000 43
0000 44 : MODIFIED BY:
0000 45
0000 46
0000 47 :--
0000 48
0000 49 : .SBTTL HISTORY                ; Detailed Current Edit History
0000 50 :
0000 51 : 3-001 Original version of complete re-write          JCW 21-DEC-82
0000 52 :

```

DECLARATIONS

```

0000 54      .SBTTL  DECLARATIONS
0000 55      :
0000 56      : INCLUDE FILES:
0000 57      :
0000 58      :     NONE
0000 59      :
0000 60      : EXTERNAL SYMBOLS:
0000 61      :
0000 62      :     .DSABL  GBL           ; Force all external symbols to be declared
0000 63      :     .EXTRN  MTH$$SIGNAL
0000 64      :     .EXTRN  MTH$K_FLOUNDMAT
0000 65      :     .EXTRN  MTH$K_INVARGMAT
0000 66      :
0000 67      : LIBRARY MACROS CALLS:
0000 68      :
0000 69      :     $$SDEF           ; Define SF$ (stack frame) symbols
0000 70      :
0000 71      : EQUATED SYMBOLS:
0000 72      :
0000 73      :     EXP 55  = ^X00001B80      ; 55*2^7
0000 74      :     HIGH_MASK = ^XFFFFFFF
0000 75      :
0000 76      : OWN STORAGE:
0000 77      :
0000 78      :     NONE
0000 79      :
0000 80      : PSECT DECLARATIONS:
0000 81      :
0000 82      :     .PSECT  _MTH$CODE      PIC, SHR, LONG, EXE, NOWRT
0000 83      :
0000 84      : CONSTANTS:
0000 85      :
0000 86      : TWO_EXP_55:
0000 87      :     .LONG  ^X00005C00, ^X0      ; 2**55
00000000 00005C00 0000

```

MTH\$DMOD - D REAL*8 remainder

```

0008 89 .SBTTL MTH$DMOD - D REAL*8 remainder
0008 90 :++
0008 91 : FUNCTIONAL DESCRIPTION:
0008 92 :
0008 93 : Return the remainder of arg1/arg2 in D floating point format
0008 94 : Remainder = arg1 - (int(arg1/arg2))*arg2
0008 95 :
0008 96 : The algorithm used to evaluate the DMOD function is as follows:
0008 97 :
0008 98 :     X = the first argument.
0008 99 :     Y = the second argument.
0008 100 : step 1. m = the exponent of Y.
0008 101 :         n = the exponent of X.
0008 102 :         c = n - m
0008 103 :         If c < 0, end with result = X.
0008 104 : step 2. I = the fractional part of X.
0008 105 :         J = the fractional part of Y.
0008 106 :         If I >= J, I = I - J
0008 107 :         Go to step 5.
0008 108 : step 3. L = 2^(p-1)*I, where p = 56 for D_floating numbers.
0008 109 : step 4. T = L/J
0008 110 :         T = [T+2^(p-1)]-2^(p-1). T is int(L/J) or int(L/J)+1
0008 111 :         I = L - J * T
0008 112 :         If I < 0, I = I + J T was int(L/J)+1
0008 113 : step 5. c = c - (p-1)
0008 114 :         If c > 0 go to step 3.
0008 115 : step 6. If c = -(p-1) go to step 9.
0008 116 : step 7. L = 2^(p-1+c) * I
0008 117 : step 8. I = L - J * T
0008 118 : step 9. Result = 2^m * I
0008 119 :
0008 120 :
0008 121 : CALLING SEQUENCE:
0008 122 :
0008 123 :     Remainder.wd.v = MTH$DMOD (dividend.rd.r, divisor.rd.r)
0008 124 :
0008 125 : INPUT PARAMETERS:
0008 126 :
0008 127 :     The two input parameters are double precision floating-point
0008 128 :     values. They are passed by reference.
0008 129 :
0008 130 :
00000004 0008 131 :     DIVIDEND = 4 ; Dividend = X in the algorithm.
00000008 0008 132 :     DIVISOR = 8 ; Divisor = Y in the algorithm.
0008 133 :
0008 134 :
0008 135 : IMPLICIT INPUTS:
0008 136 :
0008 137 :     NONE
0008 138 :
0008 139 : FUNCTION VALUE:
0008 140 :
0008 141 :     Remainder of the division of arg1/arg2 is returned as a
0008 142 :     double precision floating point value.
0008 143 :
0008 144 : IMPLICIT OUTPUTS:
0008 145 :

```

MTHSDMOD - D REAL*8 remainder

```

0008 146 : NONE
0008 147 :
0008 148 : COMPLETION CODES:
0008 149 :
0008 150 : NONE
0008 151 :
0008 152 : SIDE EFFECTS:
0008 153 :
0008 154 : MTHS_INVARGMAT - Invalid argument to math library if the divisor is zero.
0008 155 : MTHS_FLOUNDMAT - Floating underflow in math library is signaled if
0008 156 : the FU bit is set in the callers PSL.
0008 157 :
0008 158 :--
0008 159 :
01FC 0008 160 .ENTRY MTHSDMOD, ^M<R2, R3, R4, R5, R6, R7, R8>
000A 161
52 08 BC 70 000A 162 MOVD @DIVISOR(AP), R2 ; R2/R3 = Y
52 13 000E 163 BEQL ERROR ; Y=0. Division by zero
50 04 BC 70 0010 164 MOVD @DIVIDEND(AP), R0 ; R0/R1 = X
56 52 FFFF807F 8F CB 0014 165
58 50 FFFF807F 8F CB 001C 166 BICL3 #^XFFF807F, R2, R6 ; R6=m is the biased exponent of Y
0024 167 BICL3 #^XFFF807F, R0, R8 ; R8=n is the biased exponent of X
58 56 C2 0024 168 SUBL2 R6, R8 ; R4 = c = n-m unbiased
01 18 0027 169 BGEQ STEP_2 ; Result is X if X<Y, ie, if c<0
04 0029 170 RET ; R0/R1 = X
002A 171
56 DD 002A 172 STEP_2: PUSHL R6 ; push m onto the stack
002C 173
52 FF80 8F AA 002C 174 BICW2 #^XFF80, R2 ; R2/R3 = J = unbiased :fract(Y):
52 4000 8F AC 0031 175 XORW #^X4000, R2 ; J = properly biased :fract(Y):
50 FF80 8F AA 0036 176 BICW2 #^XFF80, R0 ; R0/R1 = I = unbiased :fract(X):
50 4000 8F AC 003B 177 XORW #^X4000, R0 ; I = properly biased :fract(X):
0040 178
0040 179
0040 180
0040 181 :+
0040 182 :
0040 183 : In STEP_4 and STEP_8 the calculation of I = L J*int(L/J) must be
0040 184 : computed as precisely as possible. To do this we will need to write J as
0040 185 : J = J1 + J2
0040 186 : where J1 = the high 24 bits of J and J2 = J - J1, the low 24 bits of J.
0040 187 :
0040 188 : HIGH_MASK is used to extract the 8 bits of J from longword2 that belong
0040 189 : to JT.
0040 190 :
0040 191 :--
04 AE 7E 52 7D 0040 192 MOVQ R2, -(SP) ; (SP) = J
FFFF0FFF 8F CA 0043 193 BICL #HIGH_MASK, 4(SP) ; (SP) = J1 replaces the value
; of J on the top of the SP
7E 52 6E 63 004B 194 SUBD3 (SP), R2, -(SP) ; (SP) = J2 = J - J1
52 50 71 004F 195
52 63 19 0052 196 CMPD R0, R2 ; If I<J
50 52 62 0054 197 BLSS STEP_5 ; go to STEP_5
5E 14 0057 198 SUBD2 R2, R0 ; else I = I-J
0059 199 BGTR STEP_5 ; go to STEP_5 if I>0, or
; else the algorithm ends
04 BC 85 0059 200 TSTW @DIVIDEND(AP) ; the sign of the result is
0059 201
0059 202

```

MTHSDMOD - D REAL*8 remainder

```

      50 03 18 005C 203 BGEQ DONE ; the same as the sign of
      50 50 72 005E 204 MNEGD RO, RO ; the first argument, A.
      04 0061 205 DONE: RET
      0062 206
      50 01 0F 79 0062 207 ERROR: ASHQ #15, #1, R0 ; Y=0. Reserved operand
      7E 00'8F 9A 0066 208 MOVZBL #MTH$K INVARGMAT, -(SP) ; error code
00000000'GF 01 FB 006A 209 CALLS #1, G^MTH$$SIGNAL ; signal the error
      04 0071 210 RET
      0072 211
      50 00001B80 8F C0 0072 212 STEP_3: ADDL2 #EXP_55, R0 ; R0/R1 = L = 2**(p-1)*I
      0079 213
      0079 214 :+
      0079 215 :
      0079 216 STEP 4:
      0079 217 2^(p-1) = 2^(55) is added and then subtracted from
      0079 218 T = int(L/J) to ensure that T = chopped(L/J) or chopped(L/J)+1
      0079 219 :
      0079 220 :-
      0079 221
      56 50 52 67 0079 222 DIVD3 R2, R0, R6 ; R6/R7 = T = L/J
      56 80 AF 60 007D 223 ADDD2 TWO_EXP_55, R6 ; R6/R7 = T = T+2**(p-1)
      56 FF7B CF 62 0081 224 SUBD2 TWO_EXP_55, R6 ; T-2**(p-1) = L/J chopped or choppe
      0086 225
      0086 226 :+
      0086 227 :
      0086 228 The calculation of I = L - J*int(L/J) must be computed as precisely
      0086 229 as possible. To do this we will need to write T as
      0086 230 T = Z1 + Z2
      0086 231 where Z1 = the high 24 bits of T and Z2 = T - Z1, the low 24 bits of T.
      0086 232 Now, using J = J1 + J2,
      0086 233 L - J * int(L/J) = L - (J1 + J2) * (Z1 + Z2)
      0086 234 = L - (Z1 * J1) - (Z1 * J2)
      0086 235 = L - (Z2 * J1) - (Z2 * J2)
      0086 236 = L - (Z1 * J) - (Z2 * J)
      0086 237
      0086 238
      0086 239
      0086 240 :-
      0086 241
      55 57 FFFF0FFF 8F C8 0086 242 MOVL R6, R4 ;
      0089 243 BICL3 #HIGH MASK, R7, R5 ; R4/R5 = Z1
      0091 244 SUBD2 R4, R6 ; R6/R7 = Z2
      7E 08 AE 54 62 0091 244 SUBD2 R4, R6 ;
      0094 245 MULD3 R4, 8(SP), -(SP) ; Compute Z1*J1
      0099 246 SUBD2 (SP)+, R0 ; R0/R1 = L - Z1*J1
      009C 247 MULD2 (SP), R4 ; R4/R5 = Z1*J2
      009F 248 SUBD2 R4, R0 ; R0/R1 = L - Z1*J
      54 56 08 AE 65 00A2 249 MULD3 8(SP), R6, R4 ; R4/R5 = Z2*J1
      00A7 250 SUBD2 R4, R0 ; R0/R1 = L - Z1*J - Z2*J1
      00AA 251 MULD2 (SP), R6 ; R6/R7 = Z2*J2
      00AD 252 SUBD2 R6, R0 ; R0/R1 = L - Z*J
      00B0 253 BGTR STEP 5 ;
      00B2 254 BEQL RETURN ; End if R0/R1=0
      50 52 60 00B4 255 ADDD R2, R0 ; Add J back in because you had
      00B7 256 ; T=chopped(L/J)+1
      00B7 257
      58 00001B80 8F C2 00B7 258 STEP_5: SUBL2 #EXP_55, R8 ;c = c-(p-1) = c-55
      B2 18 00BE 259 BGEQ STEP_3

```

MTHSDMOD - D REAL*8 remainder

```

58 00001B80 8F C0 00C0 260
      00C7 261
      00C7 262 :+
      00C7 263 :+
      00C7 264 :+
      00C7 265 :+
      00C7 266 :-
      00C7 267 :-
      50 42 13 00C7 268
      50 58 C0 00C9 269
      00CC 270
      00CC 271 :+
      00CC 272 :+
      00CC 273 :+
      00CC 274 :-
      00CC 275 :-
      56 50 52 67 00CC 276
      56 FF2C CF 60 00D0 277
      56 FF27 CF 62 00D5 278
      00DA 279
      00DA 280 :+
      00DA 281 :+
      00DA 282 :+
      00DA 283 :+
      00DA 284 :+
      00DA 285 :+
      00DA 286 :+
      00DA 287 :+
      00DA 288 :+
      00DA 289 :+
      00DA 290 :+
      00DA 291 :+
      00DA 292 :+
      00DA 293 :+
      00DA 294 :+
      00DA 295 :+
      00DA 296 :-
      00DA 297 :-
      55 57 FFFF0FFF 54 56 D0 00DA 298
      56 54 62 00DD 299
      7E 08 AE 54 65 00E5 300
      50 8E 62 00E8 301
      54 6E 64 00ED 302
      50 54 62 00F0 303
      54 56 08 AE 65 00F6 304
      50 54 62 00FB 305
      56 6E 64 00F8 306
      50 56 62 0101 307
      05 14 0104 308
      19 13 0106 309
      50 52 60 0108 310
      010B 311
      010B 312
      010B 313
      10 AE 4000 8F A2 010B 314
      50 10 AE A0 0111 315
      0B 19 0115 316

```

```

ADDL2 #EXP_55, R8 ; c = (p-1)+c = 55+c

The next two lines of code are STEP_6 and STEP_7.

BEQL STEP_9 ;
ADDL2 R8, R0 ; L = I*2^(c+t)

2^(p-1) = 2^(55) is added and then subtracted from
T = int(L/J) to ensure that T = chopped(L/J) or chopped(L/J)+1

DIVD3 R2, R0, R6 ; R6/R7 = T = L/J
ADD2 TWO_EXP_55, R6 ; R6/R7 = T = T+2**(p-1)
SUBD2 TWO_EXP_55, R6 ; T-2**(p-1) = L/J chopped or choppe

STEP_8:
The calculation of I = L - J*int(L/J) must be computed as precisel
as possible. To do this we will need to write T as
T = Z1 + Z2
where Z1 = the high 24 bits of T and Z2 = T - Z1, the low 24 bits of T.
Now, using J = J1 + J2,
L - J * int(L/J) = L - (J1 + J2) * (Z1 + Z2)
                  = L - (Z1 * J1) - (Z1 * J2)
                  = L - (Z2 * J1) - (Z2 * J2)
                  = L - (Z1 * J) - (Z2 * J)

MOV L R6, R4 ;
BICL3 #HIGH MASK, R7, R5 ; R4/R5 = Z1
SUBD2 R4, R6 ; R6/R7 = Z2
MULD3 R4, 8(SP), -(SP) ; Compute Z1*J1
SUBD2 (SP)+, R0 ; R0/R1 = L - Z1*J1
MULD2 (SP), R4 ; R4/R5 = Z1*J2
SUBD2 R4, R0 ; R0/R1 = L - Z1*J
MULD3 8(SP), R6, R4 ; R4/R5 = Z2*J1
SUBD2 R4, R0 ; R0/R1 = L - Z1*J - Z2*J1
MULD2 (SP), R6 ; R6/R7 = Z2*J2
SUBD2 R6, R0 ; R0/R1 = L - Z*J
BGTR STEP_9 ;
BEQL RETURN ; End if R0/R1=0
ADD R2, R0 ; Add J back in because you had
; T=chopped(L/J)+1

STEP_9: SUBW #*X4000, 16(SP) ; Remove bias from m and
ADDW2 16(SP), R0 ; form R0/R1 = 2^m*L
BLSS UNDERFLOW ; Branch if underflow

```

```

04 BC B5 0117 317 TEST_SIGN:
50 8000 05 18 0117 318 TSTW @DIVIDEND(AP) ; the sign of the result is
04 04 AD 06 E1 011A 319 BGEQ RETURN ; the same as the sign of
00000000'8F DD 011C 320 BISW2 #^X8000, R0 ; the first argument, X.
00000000'GF 01 FB 0121 321 RETURN: RET
0122 322
0122 323 UNDERFLOW:
0D 04 AD 06 E1 0122 324 CLRQ R0 ; Set up default result to 0.0
0124 325 BBC #SFSV_FU, SFSW_SAVE_PSW(FP), NO_FU
0129 326 ; Branch if caller has not enabled F
0129 327 PUSHL #MTH$K_FLOUNDMAT ; Report MTH$_FLOUNDMAT
012F 328 CALLS #1, G^MTH$$SIGNAL ; Signal the condition
04 0136 329 NO_FU: RET ; Return
0137 330
0137 331 .END

```

```

DIVIDEND      = 00000004
DIVISOR       = 00000008
DONE          = 00000061 R    02
ERROR         = 00000062 R    02
EXP_55        = 00001B80
HIGH_MASK     = FFFF0FFF
MTHSSIGNAL    ***** X    00
MTHSDMOD      00000008 RG   02
MTHSK_FLOUNDMAT ***** X    00
MTHSK_INVARGMAT ***** X    00
NO_FU         00000136 R    02
RETURN        00000121 R    02
SFSV_FU       = 00000006
SFSW_SAVE_PSW = 00000004
STEP_2        0000002A R    02
STEP_3        00000072 R    02
STEP_5        000000B7 R    02
STEP_9        0000010B R    02
TEST_SIGN     00000117 R    02
TWO_EXP_55    00000000 R    02
UNDERFLOW     00000122 R    02
    
```

! Psect synopsis !

PSECT name	Allocation	PSECT No.	Attributes
. ABS .	00000000 (0.)	00 (0.)	NOPIC USR CON ABS LCL NOSHR NOEXE NORD NOWRT NOVEC BYTE
\$ABSS	00000000 (0.)	01 (1.)	NOPIC USR CON ABS LCL NOSHR EXE RD WRT NOVEC BYTE
_MTHSCODE	00000137 (311.)	02 (2.)	PIC USR CON REL LCL SHR EXE RD NOWRT NOVEC LONG

! Performance indicators !

Phase	Page faults	CPU Time	Elapsed Time
Initialization	34	00:00:00.09	00:00:01.54
Command processing	117	00:00:00.45	00:00:03.28
Pass 1	122	00:00:01.45	00:00:05.82
Symbol table sort	0	00:00:00.03	00:00:00.19
Pass 2	72	00:00:00.71	00:00:03.37
Symbol table output	3	00:00:00.03	00:00:00.07
Psect synopsis output	3	00:00:00.02	00:00:00.02
Cross-reference output	0	00:00:00.00	00:00:00.00
Assembler run totals	353	00:00:02.79	00:00:14.30

The working set limit was 900 pages.
6542 bytes (13 pages) of virtual memory were used to buffer the intermediate code.
There were 10 pages of symbol table space allocated to hold 48 non-local and 0 local symbols.
331 source lines were read in Pass 1, producing 13 object records in Pass 2.
8 pages of virtual memory were used to define 7 macros.

! Macro library statistics !

Macro library name

Macros defined

_S255SDUA28:[SYSLIB]STARLET.MLB;2

4

88 GETS were required to define 4 macros.

There were no errors, warnings or information messages.

MACRO/ENABLE=SUPPRESSION/DISABLE=(GLOBAL,TRACEBACK)/LIS=LIS\$:MTHDMOD/OBJ=OBJ\$:MTHDMOD MSRC\$:MTHDMOD/UPDATE=(ENHS:MTHDMOD)

